

Secondary One Mathematics: An Integrated Approach

Module 1

Getting Ready

By

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Module 1 – Getting Ready

Classroom Task: Checkerboard Borders - A Develop Understanding Task

Defining quantities and interpreting expressions (N.Q.2, A.SSE.1)

Ready, Set, Go Homework: Getting Ready 1.1

Classroom Task: Building More Checkerboard Borders – A Develop Understanding Task

Defining quantities and interpreting expressions (N.Q.2, A.SSE.1)

Ready, Set, Go Homework: Getting Ready 1.2

Classroom Task: Serving Up Symbols – A Develop Understanding Task

Interpreting expressions and using units to understand problems (A.SSE.1, N.Q.1)

Ready, Set, Go Homework: Getting Ready 1.3

Classroom Task: Examining Units – A Solidify Understanding Task

Using units as a way to understand problems (N.Q.1)

Ready, Set, Go Homework: Getting Ready 1.4

Classroom Task: Cafeteria Actions and Reactions – A Develop Understanding Task

Explaining each step in the process of solving an equation (A.REI.1)

Ready, Set, Go Homework: Getting Ready 1.5

Classroom Task: Elvira’s Equations – A Solidify Understanding Task

Rearranging formulas to solve for a variable (A.REI.3, A.CED.4)

Ready, Set, Go Homework: Getting Ready 1.6

Classroom Task: Solving Equations, Literally – A Practice Understanding Task

Solving literal equations (A.REI.1, A.REI.3, A.CED.4)

Ready, Set, Go Homework: Getting Ready 1.7

Classroom Task: Cafeteria Conundrums – A Develop Understanding Task

Writing inequalities to fit a context (A.REI.1, A.REI.3)

Ready, Set, Go Homework: Getting Ready 1.8

Classroom Task: Greater Than? – A Solidify Understanding Task

Reasoning about inequalities and the properties of inequalities (A.REI.1, A.REI.3)

Ready, Set, Go Homework: Getting Ready 1.9

Classroom Task: Taking Sides – A Practice Understanding Task

Solving linear inequalities and representing the solution (A.REI.1, A.REI.3)

Ready, Set, Go Homework: Getting Ready 1.10

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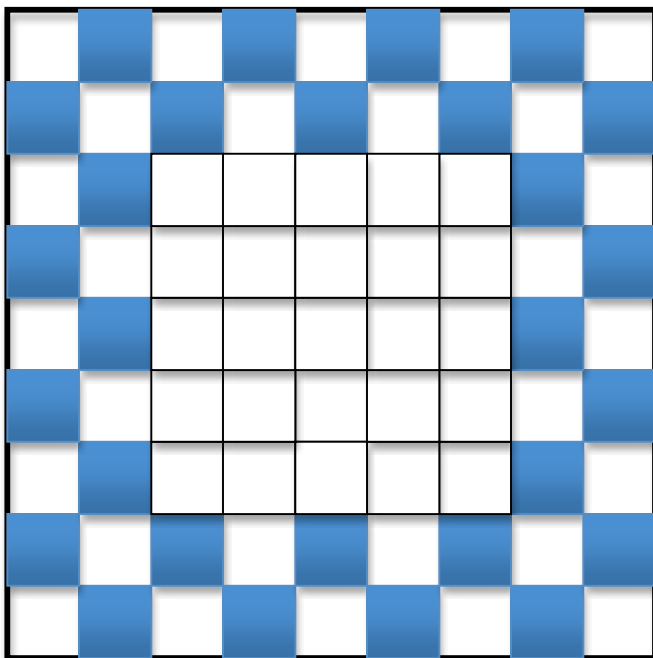
1.1 Checkerboard Borders

A Develop Understanding Task

In preparation for back to school, the school administration has planned to replace the tile in the cafeteria. They would like to have a checkerboard pattern of tiles two rows wide as a surround for the tables and serving carts.

Below is an example of the border that the administration is thinking of using to surround a square 5 x 5 set of tiles.

- A. Find the number of colored tiles in the checkerboard border. Track your thinking and find a way of calculating the number of colored tiles in the border that is quick and efficient. Be prepared to share your strategy and justify your work.



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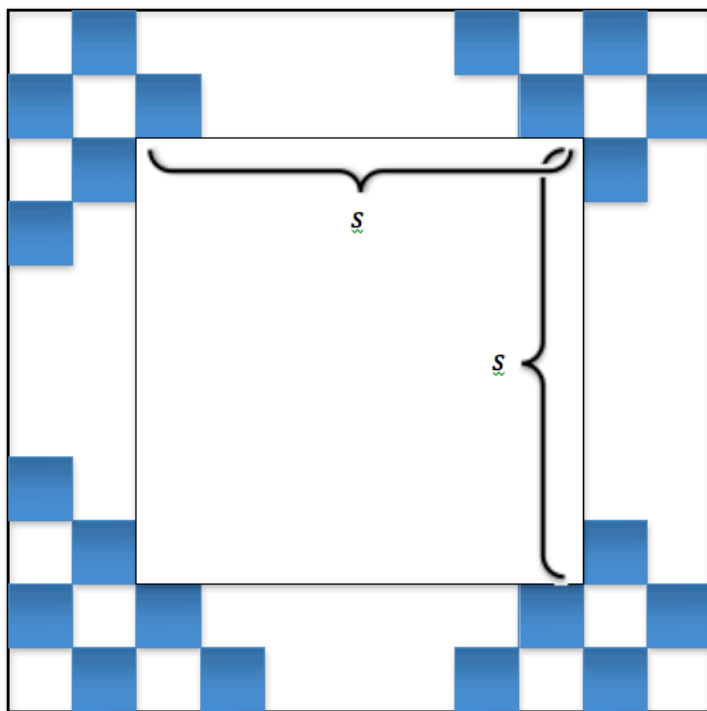
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- B. The contractor that was hired to lay the tile in the cafeteria is trying to generalize a way to calculate the number of colored tiles needed for a checkerboard border surrounding a square of tiles with dimensions $s \times s$. Find an expression for the number of colored border tiles needed for any $s \times s$ square center.



1.1 Checkerboard Borders – Teacher Notes

A Develop Understanding Task

Purpose: The focus of this task is on the generation of multiple expressions that connect with the visuals provided for the checkerboard borders. These expressions will also provide opportunity to discuss equivalent expressions and review the skills students have previously learned about simplifying expressions and the using variables.

Core Standards Focus:

N.Q.2 Define appropriate quantities for the purpose of descriptive modeling.

A.SSE.1 Interpret expressions that represent a quantity in terms of its context. ★

- a. Interpret parts of an expression, such as terms, factors, and coefficients.
- b. Interpret complicated expressions by viewing one or more of their parts as a single entity.

Related Standards: A.CED.2, A.REI.1

Launch (Whole Class):

After reading and discussing the “Checkerboard Borders” scenario, challenge students to come up with a way to quickly count the number of colored tiles in the border. Have them create numeric expressions that exemplify their process and require them to connect their thinking to the visual representation of the tiles.

The first phase of work should be done individually, allowing students to “see” the problem and patterns in the tiles in their own way. This will provide for more representations to be considered later. After students work individually for a few minutes on part A, have them share with a partner and begin to develop additional ideas as a pair or assist each other in generalizing their strategy for part B.

Explore (Individual then pairs):

For students who don’t know where to begin, it may be useful to ask some starter questions like: “How many tiles are there along one side?”, “How can you count the tiles in groups rather than one-by-one?”

Press on students to connect their numeric representations to the visual representation. You might ask, “How does that four in your number sentence connect to the visual representation?” Encourage students to mark on the visual or to redraw it so they can demonstrate how they were thinking about the diagram numerically.

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Watch for students who calculate the number of border tiles in different ways. Make note of their numeric strategies and the different generalized expressions that are created. The differing strategies and algebraic expressions will be the focus of the discussion at the end, allowing for students to connect back to prior work from previous mathematical experiences and better understand equivalence between expressions and how to properly simplify an algebraic expression. Prompt students to calculate the number of tiles for a given side length using their expression and then to draw the visual model and check for accuracy. Require students to justify why their expression will work for any side length S of the inner square region. Press them to generalize their justifications rather than just repeat the process they have been using. You might ask, “How do you know your expression will work for any side length?”, or “What is it about the nature of the pattern that suggests this will always work?”, or “What will happen if we look at a side length of six? ten? fifty-three?” Consider these ideas both visually and in terms of the general expression.

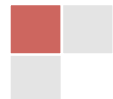
Note: Based on the student work and the difficulties they may or may not encounter, a determination will need to be made as to whether a discussion of part A of the task should be held prior to students working on part B. Working with a specific case may facilitate access to the general case for more students. However, if students are ready for whole class discussion of their general representations, then starting there will allow for more time to be spent on making connections between the different expressions, and extending the task to more general representations.

As available, select students to present who found different ways of generalizing. Some possible ways students might “see” the colored tiles grouped are provided below. It would be good to have at least three different views to discuss and possibly more.

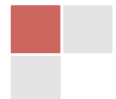
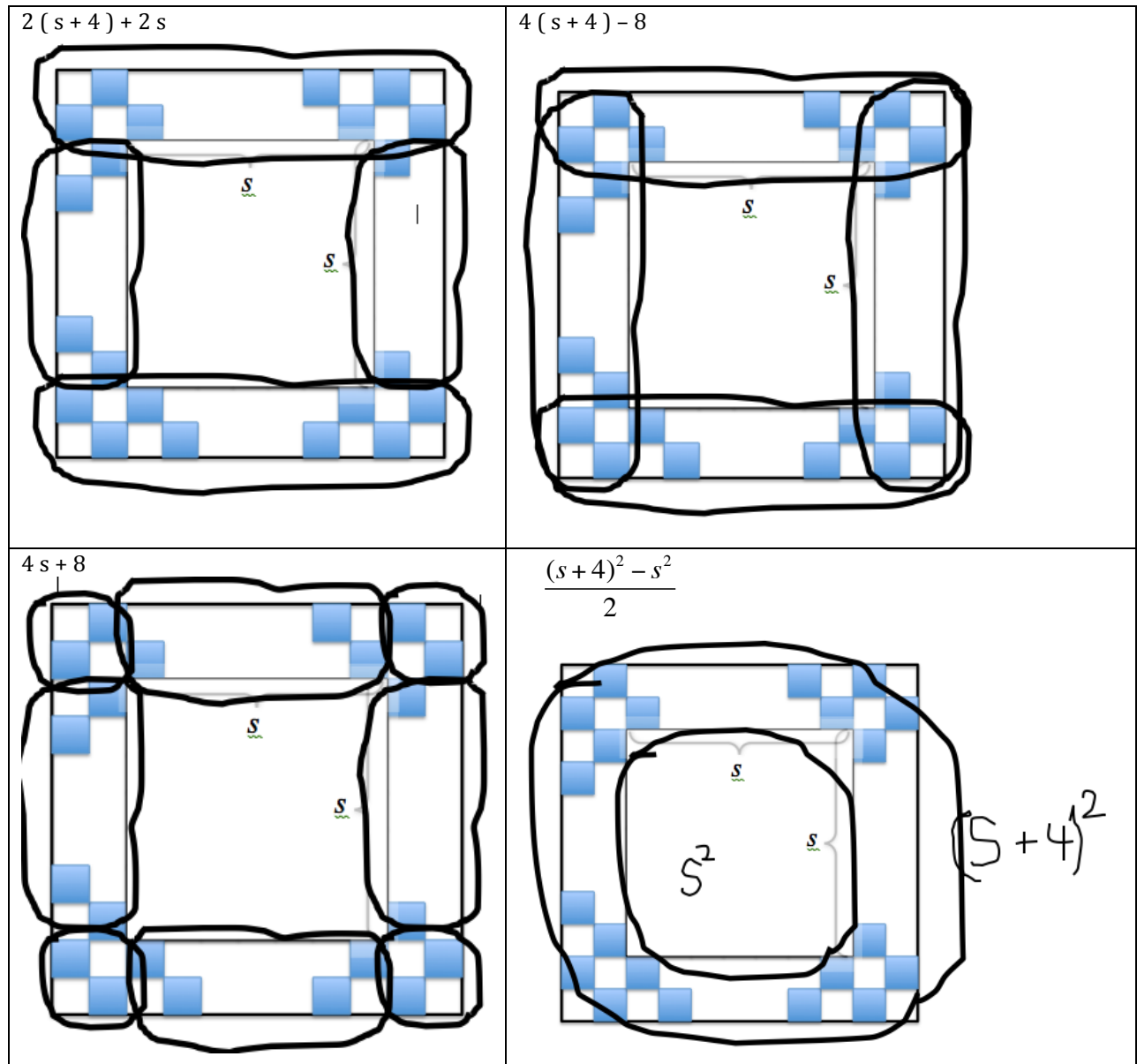
Discuss (Whole Class):

Based on the student work available you will need to determine the order of the strategies to be presented. A likely progression would start with a strategy that does not provide the most simplified form of the expression. This will promote questioning and understanding from students that may have done it differently and allow for discussion about what each piece of the expression represents. After a couple of different strategies have been shared it might be good to get the most simplified form of the expression out on the table and then look for an explanation as to how all of the expressions can be equivalent and represent the same thing in so many different ways.

Aligned Ready, Set, Go: Getting Ready 1.1



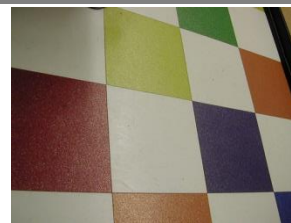
Possible student strategies:



Name: _____

Getting Ready | 1.1

Ready, Set, Go!



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Ready

Topic: Solve one variable equations

Find the value of x that makes each equation true.

1. $6x = 18$

2. $3x - 10 = 2$

3. $8x - 10 = x + 11$

4. $5x - 7 = 7x - 17$

5. $3x + 9 = 44 - 2x$

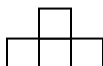
6. $3x + 6 = x + 2$

Set

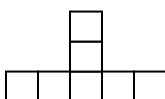
Topic: Create and solve equations in one variable.

Use the pictures below to answer questions 7 – 12.

Step 1



Step 2



Step 3

7. Each square represents one tile, how many total tiles are in Step 5? Step 6?
8. What might you do to determine the number of tiles in Step 25?
9. Write a rule to predict the total number of tiles for any step. Show how your rule relates to the pattern.
10. Try to think of a different rule that you can use to predict the total number of tiles for any step. Show how your rule relates to the pattern.
11. Andrew also solved this problem and came up with following equation: $s = 1 + 3(n-1)$. How does each piece of his expression show up in the pattern?
12. Tami came up with the equation $s = 3n - 2$. How does each piece of her expression show up in the pattern?

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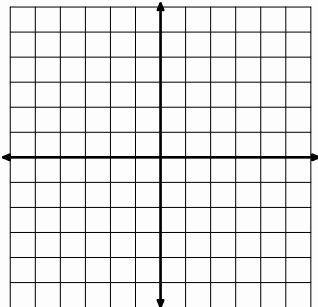


Go

Topic: Graph linear equations

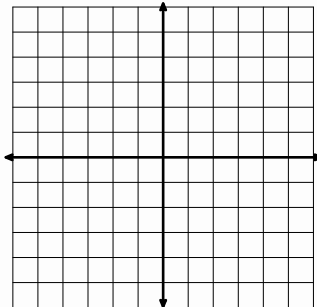
For the following problems two points and a slope are given. Use the graph to plot these points, draw the line, and *clearly* label the slope on the graph.

13. $(2, -1)$ and $(4, 2)$



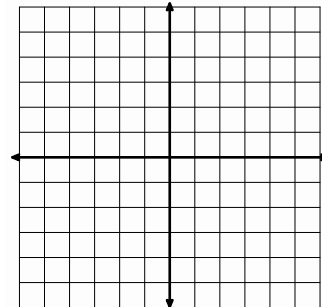
Slope: $m = \frac{3}{2}$

14. $(-2, 1)$ and $(2, 5)$



Slope: $m = 1$

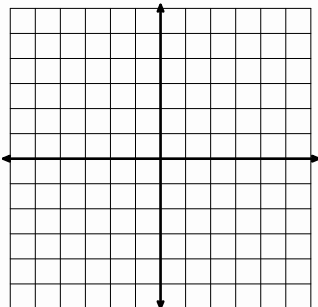
15. $(0, 0)$ and $(3, 6)$



Slope: $m = 2$

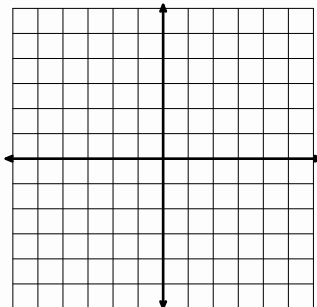
For the following problems, two points are given. Use the graph to plot these points *and* find the slope.

16. $(-3, 0)$ and $(0, 5)$



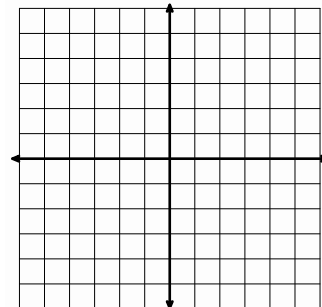
Slope: $m =$

17. $(-2, -1)$ and $(-4, 4)$



Slope: $m =$

18. $(0, 3)$ and $(1, 6)$



Slope: $m =$

Need Help? Check out these related videos:

<http://www.khanacademy.org/math/algebra/solving-linear-equations/v/solving-equations-1>

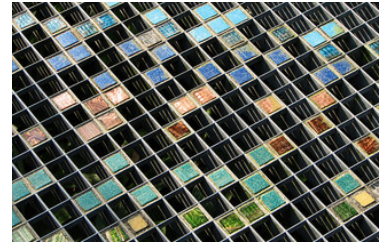
<http://www.khanacademy.org/math/algebra/linear-equations-and-inequalities/v/graphing-a-line-in-slope-intercept-form>

<http://www.youtube.com/watch?v=WXzpisUh0AU>



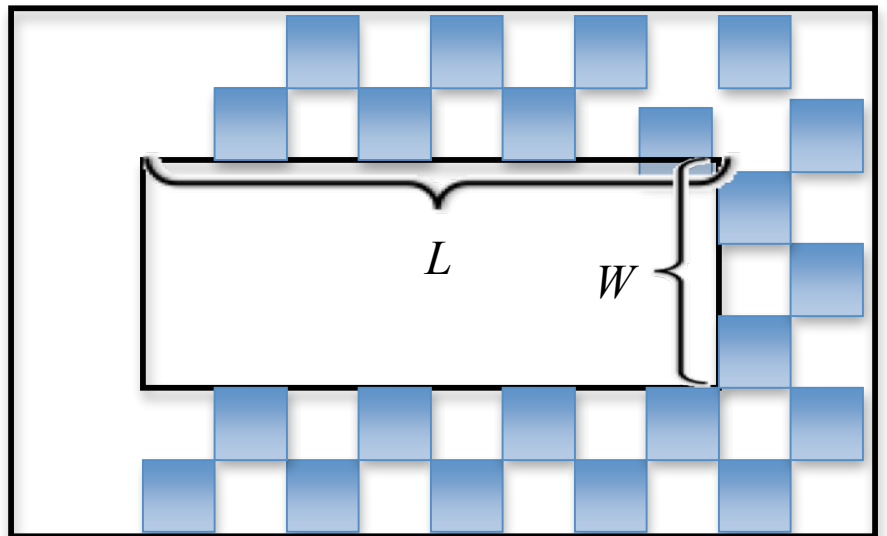
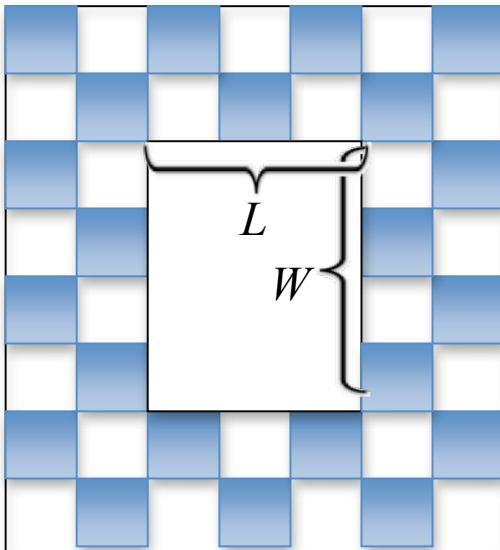
1.2 Building More Checkerboard Borders

A Develop Understanding Task



As the tile workers started to look more deeply into their work they found it necessary to develop a way to quickly calculate the number of colored border tiles for not just square arrangements but also for checkerboard borders to surround any $L \times W$ rectangular tile center.

Find an expression to calculate the number of colored tiles in the two row checkerboard border for any rectangle. Be prepared to share your strategy and justify your work. Create models to assist you in your work.



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1.2 Building More Checkerboard Borders- Teacher Notes

A Develop Understanding Task

Purpose: Building on the previous task, the focus of this task is on the generation of multiple expressions that connect with the visuals provided for the checkerboard borders. These expressions will also provide opportunity to discuss the incorporation of two variables, in this case L and W . This task could be used the same day as the Checkerboard Borders task or the following day based on students' needs.

Core Standards Focus:

CCSSM Integrated Pathway Math 1: Critical Area 2

“... interpret given [expressions] graphically, numerically, symbolically, and verbally, translate between representations, and understand the limitations of various representations.”

N.Q.2 Define appropriate quantities for the purpose of descriptive modeling.

A.SSE.1 Interpret expressions that represent a quantity in terms of its context.★

- a. Interpret parts of an expression, such as terms, factors, and coefficients.
- b. Interpret complicated expressions by viewing one or more of their parts as a single entity.

Related Standards: **A.CED.2, A.REI.1**

Launch (Whole Class):

After reading and discussing the “Building More Checkerboard Borders” scenario, challenge students to come up with a way to count the number of colored tiles in the border. Allow students time to work individually for a few minutes to allow them time to reflect on their work in the previous task and develop an algebraic expression.

Explore (Small Group):

For students who don't know where to begin, it may be useful to ask some starter questions like, “How did you find the number of colored tiles in ‘Checkerboard Borders?’” or “How do the number of colored tiles along one side of the rectangle compare with the length of that side?”

Press on students to connect their algebraic representations to the visual representation. You might ask, “How does that 2 in your number sentence connect to the visual representation?” Encourage students to mark on the visual or to redraw it so that it shows how they were thinking about it numerically.

Watch for students who calculate the colored border tiles in different ways. Make note of their strategies and the different generalized expressions that are created. The differing strategies and algebraic expressions will be part of the discussion at the end, allowing for students to connect back

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to prior work from previous mathematical experiences and better understand equivalence between expressions and how to properly simplify an algebraic expression. Prompt students to calculate the number of tiles for given a length and width using their expression and then to draw the visual model and check for accuracy. Require students to justify why their expression will work for any length L and width W for an inner rectangular region. Press them to generalize their justifications rather than just repeat the process they have been using. You might ask, "How do you know that expression will work for any side length?", or "What is it about the nature of the pattern that suggests this will always work?", "What will happen if we look at a side length of six and a width of 9? ten? fifty-three?" Consider this both visually and in terms of the general expression.

Discuss (Whole Class):

As available, select students to present who found different ways of generalizing. Some possible ways students might "see" the colored tiles grouped are provided below. It would be good to have at least three different views to discuss and possibly more.

Possible student strategies: (these can be comparable to those in Checkerboard Borders)

$2(L + 4) + 2W$	$2(L + 4) + 2(W + 4) - 8$
$2L + 2W + 8$	$\frac{(L + 4)(W + 4) - LW}{2}$

Aligned Ready, Set, Go: Getting Ready 1.2



Name: _____

Getting Ready | 1.2

Ready, Set, Go!



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Ready

Solve the following equations for the unknown variable.

1. $4(x + 3) = 1$

2. $q - 13 = -13$

3. $21s = 3$

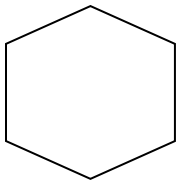
4. $\frac{7f}{11} = \frac{7}{11}$

5. $5q - 7 = \frac{2}{3}$

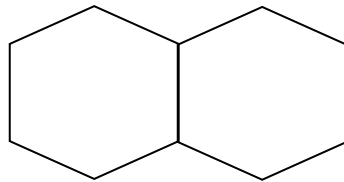
6. $5x - (3x + 2) = 1$

Set

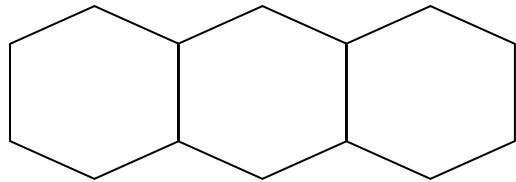
For the growing pattern below, each line segment is one unit in length.



Step 1



Step 2



Step 3

7. How much total **perimeter** in Step 5? Step 6? (Remember to focus on the perimeter.)
8. How can you determine the amount of perimeter in Step 25?
9. Write a rule to predict the total amount of perimeter for any step. Show how your rule relates to the pattern.
10. Marsha also solved this problem and came up with following expression: $1 + 5n - (n-1)$. How does each piece of her expression show up in the pattern?
11. Tyler came up with the expression $6n - 2(n-1)$. How does each piece of his expression show up in the pattern?

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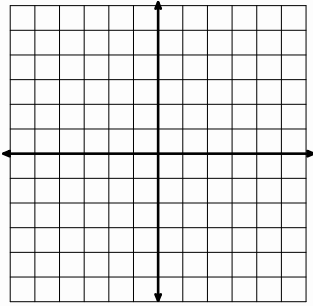
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Getting Ready | 1.2

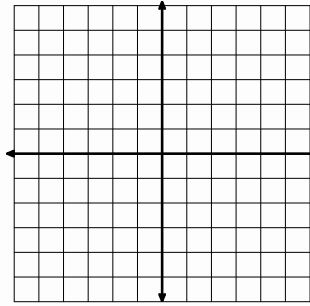
Go

For problems 12 and 13, the y-intercept and the slope of a line are given. Graph the line on the coordinate axes, clearly labeling the slope and y-intercept.

12. $(0, 2); m = \frac{3}{4}$



13. $(0, -3); m = 4$



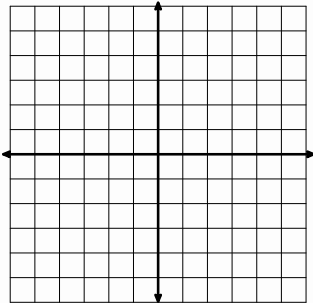
The equations below are represented in the above graphs. Explain how the slope and y-intercept show up in both the graph and algebraic representations.

$$y = \frac{3}{4}x + 2$$

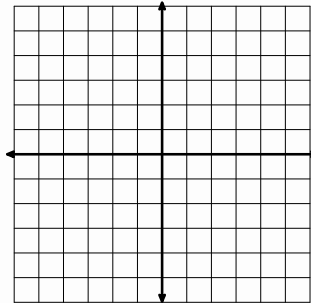
$$y = 4x - 3$$

For problems 14-16, graph the following equations on the provided coordinate axes.

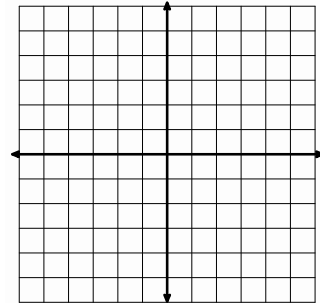
14. $y = 2x - 1$



15. $y = \frac{1}{3}x + 2$



16. $y = -3x + 5$



Need Help? Check out these related videos:

<http://www.khanacademy.org/math/algebra/solving-linear-equations/v/solving-equations-1>

<http://www.khanacademy.org/math/algebra/linear-equations-and-inequalities/v/graphing-a-line-in-slope-intercept-form>

<http://www.youtube.com/watch?v=WxzpisUh0AU>

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1.3 Serving Up Symbols

A Develop Understanding Task

As you look around your school cafeteria, you may see many things that could be counted or measured. To increase the efficiency of the cafeteria, the cafeteria manager, Elvira, decided to take a close look at the management of the cafeteria and think about all the components that affect the way the cafeteria runs. To make it easy, she assigned symbols for each count or measurement that she wanted to consider, and made the following table:



Symbol	Meaning (description of what the symbol means in context)	Units (what is counted or measured)
<i>S</i>	Number of students that buy lunch in the cafeteria each day	<i>students</i> or <i>students/day</i>
<i>S_M</i>	Number of students who have passed through a line in <i>M</i> minutes	
<i>C</i>	Number of classes per lunch period	□
<i>P</i>	Number of lunch periods per day	
<i>B</i>	Number of boys that buy lunch each day	<i>boys</i> or <i>students</i> or <i>boys/day</i>
<i>G</i>	Number of girls that buy lunch each day	
<i>F</i>	Number of food servers in the cafeteria	
<i>T</i>	Total number of food items in one lunch (Each entrée, side dish, or beverage counts as 1 item.)	□
<i>M</i>	Number of minutes passed since the beginning of the lunch period	
<i>N_e</i>	Number of entrees in each lunch	
<i>N_s</i>	Number of side dishes in each lunch	
<i>N_b</i>	Number of beverages in each lunch	
<i>C_e</i>	Cost of each entrée	
<i>C_s</i>	Cost of each side dish	
<i>C_b</i>	Cost of each beverage	
<i>L</i>	Number of lines in the cafeteria	
<i>W</i>	The number of food servers per line	
<i>i</i>	Average number of food items that a server can serve each minute (Each entrée, side dish, or beverage counts as 1 item.)	
<i>H</i>	Number of hours each food server works each day	
<i>P_L</i>	Price per lunch	



Using the given symbols, it is possible to write many different algebraic expressions.

- Using these symbols, what would the expression $\frac{G+B}{C \times P}$ mean?
- Using these symbols, what would the expression $S + F + L$ mean?

Elvira hopes to use the symbols in the chart to come up with some meaningful expressions that will allow her to analyze her cafeteria. Your job is to help her by writing as many expressions as you can and describe what they mean. Put each of your expressions in the following chart, adding lines if you need to:

Expression	Description

Write an expression for the average number of lunches served in a line each day.

Write an expression for the total price of the items served in a line.



1.3 Serving Up Symbols – Teacher Notes

A Develop Understanding Task

Purpose: The purpose of the task is to develop understanding of the use of variables given a story context. Students are asked to interpret expressions written with variables, which will open up strategies for using units to analyze expressions. Students will also combine variables to make meaningful expressions and describe the meaning of the expressions they have written.

In mathematics, things we can count or measure are referred to as “quantities”. The references we use to count or measure those things are called “units”. When modeling a situation mathematically, two questions that generally arise are “What are we going to count or measure,” and “What units will we use to count or measure those things?” In this task, students work with quantities and units.

Core Standards:

A.SSE.1 Interpret expressions that represent a quantity in terms of its context.

- Interpret parts of an expression, such as terms, factors, and coefficients.
- Interpret complicated expressions by viewing one or more of their parts as a single entity. *For example, interpret $P(1+r)^n$ as the product of P and a factor not depending on P .*

N.Q.1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas.

Launch (Whole Class): Start by familiarizing students with the context of the problem. Before giving the task to students, ask them to think of some of the things that could be counted or measured in the cafeteria. Hand out the task and ask them to read through the list of variables identified by the cafeteria manager to see if they can find the things that they thought of. You may need to explain the use of subscripts for some of the variables, since many students may not have used them previously. Have students consider the units they might use to count or measure the quantities being described, and have them enter these units in the third column of the chart. Note that the given examples suggest that we can change units on a quantity if it is helpful in thinking about computation. For example, “boys that each lunch in the cafeteria each day” could be measured in units such as: boys/day, boys or students.

Introduce students to the idea that variables can be combined to make meaningful expressions.

Using question #1, ask students what the expression $\frac{G+B}{C \times P}$ means. Help students to break down the various parts of the expression. In this case, $G + B$ represents the number of students that eat lunch in the cafeteria each day. Since C represents the number of classes per lunch period and P represents the number of lunch periods, $C \times P$ represents the number of classes and the expression $\frac{G+B}{C \times P}$ represents the average number of students served lunches per class.



Give students a few minutes to think individually about the meaning of #2, $S + F + L$. After they have translated each of the variables, ask what they believe the sum of these expressions means. They should recognize that the expression formed by adding these variables doesn't make sense.

Introduce their task, which is to write as many meaningful expressions as they can. As they have seen in #2, they must be careful to combine the variables with operations that make sense in the context.

Explore (Small Group or Pairs): Assign students to work on the remainder of the task. Monitor their work, pressing students to make sense of each expression they write. Encourage students to use as many of the variables as they can in their expressions. Be prepared to record interesting expressions and their descriptions so that they can be used later in the discussion.

Discuss (Whole Group): Using the expressions that students have written, facilitate the first part of the discussion by giving several expressions, one at a time, and asking the whole class to interpret them. Switch to giving the students several descriptions that students have written and see if the class can come up with an expression that goes with it. Ask students to volunteer the most complicated meaningful expression they could create.

Close the discussion with the last two questions. There may be several different expressions for each of the questions. If this occurs, ask students if the expressions are equivalent, and how they know.

Aligned Ready, Set, Go: Getting Ready 1.3



Name:

Getting Ready | 1.3

Ready, Set, Go!



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Ready

Topic: Evaluating Expressions

Evaluate the following expressions for $a = -3$, $b = 2$, $c = 5$, and $d = -4$.

1. $2a + 3b$

2. $4c + d$

3. $5ac - 2b$

4. $\frac{2a}{c-d}$

5. $\frac{3b}{d}$

6. $\frac{a-4b}{3c+2d}$

The equation $c = 2000 + 3r$ represents the cost in dollars (c) of producing remote controls (r).

7. What is the cost of producing 1000 remote controls?

8. What is the cost of producing 2000 remote controls?

9. What is the cost of producing 2500 remote controls?

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Name:

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Set*Solve each equation, justifying each step you use.*

10.

$3x = 15$	Justification

11.

$x - 10 = 2$	Justification

12.

$-16 = x + 11$	Justification

13.

$6 - x = 10$	Justification

14.

$6x + 3 = 15$	Justification

15.

$3x - 10 = 2$	Justification



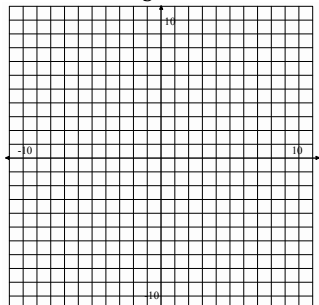
Name: _____

Getting Ready | 1.3

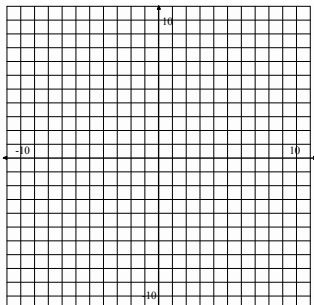
Go

Graph the following equations on the provided coordinate grids.

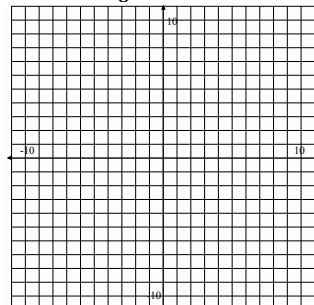
16. $y = -\frac{3}{5}x + 7$



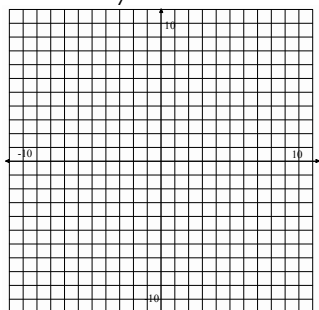
17. $y = -2x + 1$



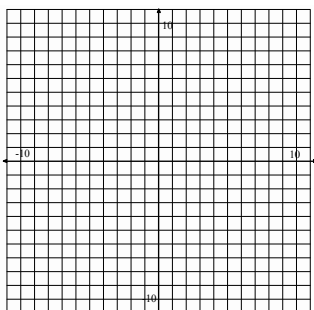
18. $y = \frac{5}{8}x + 1$



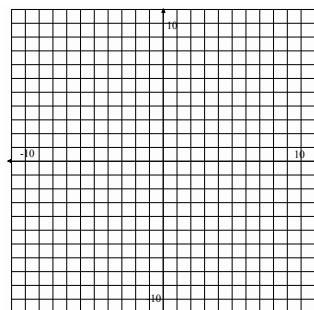
19. $y = \frac{6}{7}x$



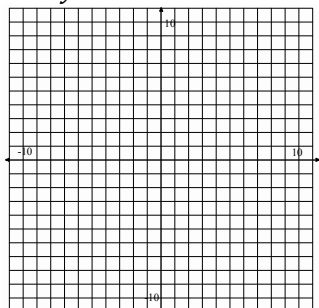
20. $y = x - 3$



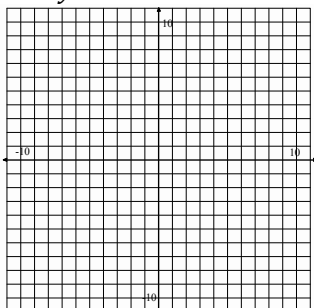
21. $y = 4x$



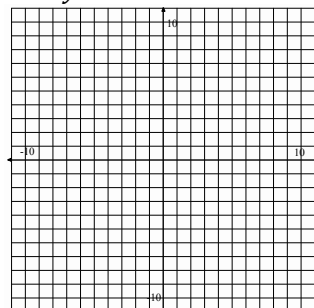
22. $y = -x - 6$



23. $y = 3x + 2$



24. $y = x$



Need Help? Check out these related videos:

<http://www.khanacademy.org/math/algebra/solving-linear-equations/v/solving-equations-1>
<http://www.khanacademy.org/math/algebra/linear-equations-and-inequalities/v/graphing-a-line-in-slope-intercept-form>
<http://www.youtube.com/watch?v=WXzpisUh0AU>

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1.4 Examining Units

A Solidify Understanding Task

(Note: This task refers to the same set of variables as used in *Serving Up Symbols*)



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Units in Addition and Subtraction

1. Why can you add $N_e + N_s + N_b$ and you can add $B + G$, but you can't add $M + W$?
2. We measure real-world quantities in units like feet, gallons, students and miles/hour (miles per hour).
 - a. What units might you use to measure N_e , N_s and N_b ?
What about the sum $N_e + N_s + N_b$?
 - b. What units might you use to measure B ? G ?
What about the sum $B + G$?
 - c. What units might you use to measure M ? W ?
What about the sum $M + W$?
3. State a rule about how you might use units to help you think about what types of quantities can be added. How would you use or modify your rule to fit subtraction?

Units in Multiplication, scenario 1

1. Why can you multiply $N_e \times C_e$ and you can multiply $L \times W$, but you can't multiply $G \times C$?
2. Units in multiplication often involve rates like miles/gallon (miles per gallon), feet/second (feet per second), or students/table (students per table).
 - a. What units might you use to measure N_e ? C_e ?
What about the product $N_e \times C_e$?
 - b. What units might you use to measure L ? W ?
What about the product $L \times W$?
 - c. What units might you use to measure G ? C ?
What about the product $G \times C$?
3. State a rule about how you might use units to help you think about what types of quantities can be multiplied.



Units in Multiplication, scenario 2

1. Let ℓ represent the length of the cafeteria in feet and w represent its width in feet. What does $\ell + w + \ell + w$ represent? What about $\ell \times w$?
2. Why can we add $\ell + w$ and multiply $\ell \times w$? What is it about these variables that allow them to be added or multiplied?
3. How might you modify your rule for using units to guide your thinking when multiplying?

Units in Division, scenario 1

1. What are the units for the **dividend** (what you are dividing up), the **divisor** (what you are dividing by) and the **quotient** (the result of the division) in the following expressions:

a. $\frac{S}{P}$

b. $\frac{F}{L}$

c. $\frac{S}{F}$

d. $\frac{S_M}{M}$

2. State a rule about the units in division problems like those represented above.

Units in Division, scenario 2

1. What are the units for the dividend (what you are dividing up), the divisor (what you are dividing by) and the quotient (the result of the division) in the following expressions:

a. $\frac{F}{W}$

b. $\frac{P_L}{T}$

2. State a rule about the units in division problems like those represented above.



1.4 Examining Units – Teacher Notes

A Solidify Understanding Task

Purpose: Quantities are measured in units. When quantities are added, subtracted, multiplied or divided the units on the result of the operation may be different from the units used to measure the individual quantities. The new units formed are a consequence of the meaning of the operations. For example, if the amount of gasoline I put in my car is measured in gallons, and the distance I travel when using up that amount of gasoline is measured in miles, then a new unit of measure, miles per gallon, emerges to measure the efficiency of my car’s usage of gasoline. This is a result of dividing the number of gallons of gasoline used by the number of miles driven. In this task students solidify the use of units as a tool for understanding problems and as a guide for determining what operations make sense when combining quantities using the four basic arithmetic operations.

Core Standards Focus:

N.Q.1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas.

Related Standards: N.Q.2, A.SSE.1

Launch (Whole Class):

Provide a model for the type of thinking expected of students on this task by working through the first section of the task, “Units in Addition and Subtraction”, together as a class. The key idea to emerge here is that we have to measure quantities with “like” units before we can add or subtract them. For example, we may refer to the quantities represented by N_e as “entrées”, N_s as “side dishes” and N_b as “beverages” when thought of separately, but we think of them as “items” when we consider their sum. Similarly we might refer to the quantity represented by B as “boys” and G as “girls”, but we measure the sum $B+G$ as “students” or “people”. In order to add or subtract quantities we have to be able to reconsider them in terms of “like” units such as people, or items, or fruits (as in 2 apples + 3 oranges = 5 fruits).

As students consider the operations of multiplication and division in the remainder of the task, encourage them to write out the units on each factor or term. They will have to carefully assign, and maybe reassign, units to the quantities being represented by the “Serving up Symbols” variables. For example, in various contexts the variable B may be measured with the units “boys”, “students” or “boys per day”.



Explore (Small Group):

Key issues for students to notice about units in multiplication:

Unlike addition, the two factors in multiplication generally play different roles. Sometimes one factor specifies the number of groups, and the other factor specifies the amount in the group. In terms of units, the factor that represents the number of groups is generally a single unit, such as “lines” or “hours”; the unit on the factor that represents the amount in a group is generally a rate, such as “workers per line” or “items per hour”. Sometimes the two factors each represent different rates, and the product describes a third rate. Other times the factors might represent linear units, and then the product represents square units. In each case, there has to be some common unit that “cancels” or makes sense when multiplied by itself as a square or cubic unit.

- We can multiply $(N_e \text{ entrées/lunch}) \times (C_e \text{ dollars/entrée})$ and the product will be measured in *dollars/lunch*.
- We can multiply $(L \text{ lines} \times W \text{ workers/line})$ and the product will be measured in *workers*.
- We cannot multiply $(G \text{ girls/day} \times C \text{ classes/lunch period})$.
- We can multiply $(l \text{ feet}) \times (w \text{ feet})$ and the product is measured in *square feet*.

Key issues for students to notice about units in division:

When a dividend is measured with a single unit such as “miles” or “students” and the divisor is measured by a single unit like “hours” or “serving lines” or “teachers” the quotient can represent a rate (miles per hour), an average (people per serving line) or a ratio (students per teacher).

We can divide a unit of measure by a rate involving that unit of measure, providing the unit of measure will “cancel”.

- We can divide S students by P lunch periods and the quotient will measure the average number of *students per lunch period*.
- We can divide F servers by L lines and the quotient will measure the average number of *servers per line*.
- We can divide S students by F food servers and the quotient will measure the ratio of *students per food server*.
- We can divide S_M students by M minutes and the quotient will measure the rate of *students per minute*.
- We can divide F servers by W servers/line and the quotient will determine the number of *lines*.
- We can divide P_L dollars/lunch by T items/lunch and the quotient will give the average *dollars/item*.

Discuss (Whole Class):

The discussion should examine the key issues listed above.

Aligned Ready, Set, Go: Getting Ready 1.4



Name:

Getting Ready 4

Ready, Set, Go!



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Ready

Topic: Solve and justify one variable equations

Solve each equation, justifying each step you use.

1. $8x - 10 = x + 11$	Justification	2. $5p - 2 = 32$	Justification
3. $10(y + 5) = 10$	Justification	4. $3x + 9 = 44 - 2x$	Justification

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Set

Topic: Understanding variables

Use the task **Serving Up Symbols** to complete the table below.

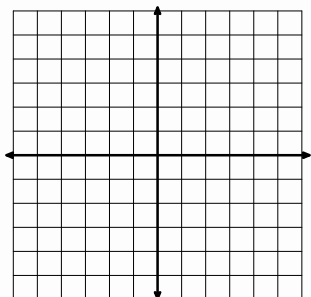
Expression	Description
$\frac{C}{L}$	
$\frac{C}{W}$	
$\frac{F}{L}$	
	Total beverages served in the cafeteria per day
	Average number of food items per week
	The average number of food items served per minute

Go

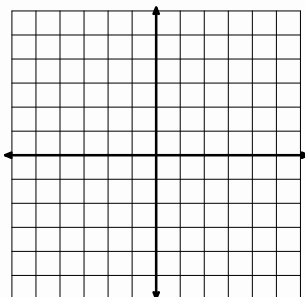
Topic: Graph linear equations

Graph each equation.

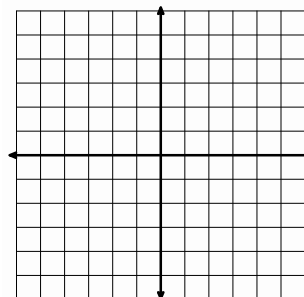
6. $y = 3x + 1$



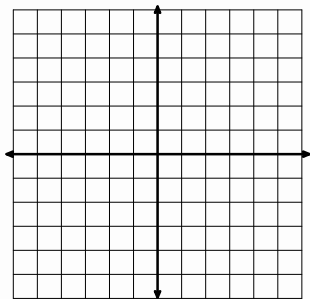
7. $y = -2x + 3$



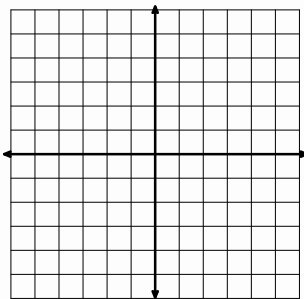
8. $y = \frac{1}{2}x - 5$



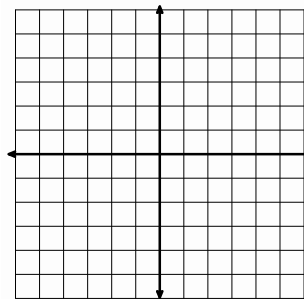
9. $y = -\frac{2}{3}x + 2$



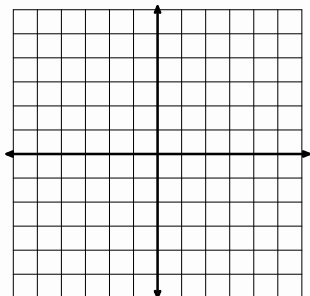
10. $y = 2x - 1$



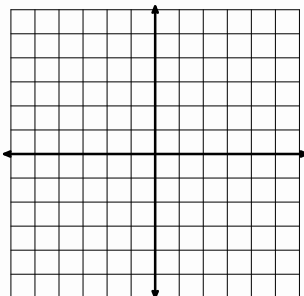
11. $y = -\frac{1}{2}x + 4$



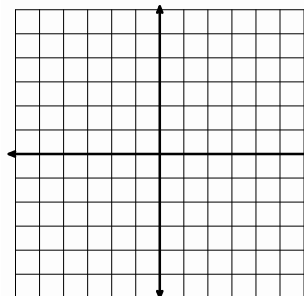
12. $y = 4x + 2$



13. $y = 2x$



14. $y = -3x + 5$



Need help? Check out these related videos:

<http://www.khanacademy.org/math/algebra/solving-linear-equations/v/solving-equations-1>

<http://www.khanacademy.org/math/algebra/linear-equations-and-inequalitie/v/graphing-a-line-in-slope-intercept-form>

<http://www.youtube.com/watch?v=WXzpisUh0AU>

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1.5 Cafeteria Actions and Reactions

A Develop Understanding Task

Elvira, the cafeteria manager, has just received a shipment of new trays with the school logo prominently displayed in the middle of the tray. After unloading 4 cartons of trays in the pizza line, she realizes that students are arriving for lunch and she will have to wait until lunch is over before unloading the remaining cartons. The new trays are very popular and in just a couple of minutes 24 students have passed through the pizza line and are showing off the school logo on the trays. At this time, Elvira decides to divide the remaining trays in the pizza line into 3 equal groups so she can also place some in the salad line and the sandwich line, hoping to attract students to the other lines. After doing so, she realizes that each of the three serving lines has only 12 of the new trays.



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“That’s not many trays for each line. I wonder how many trays there were in each of the cartons I unloaded?”

1. Can you help the cafeteria manager answer her question using the data in the story about each of the actions she took? Explain how you arrive at your solution.

Elvira is interested in collecting data about how many students use each of the tables during each lunch period. She has recorded some data on Post-It Notes to analyze later. Here are the notes she has recorded:

- Some students are sitting at the front table. (I got distracted by an incident in the back of the lunchroom, and forgot to record how many students.)
- Each of the students at the front table has been joined by a friend, doubling the number of students at the table.
- Four more students have just taken seats with the students at the front table.
- The students at the front table separated into three equal-sized groups and then two groups left, leaving only one-third of the students at the table.
- As the lunch period ends, there are still 12 students seated at the front table.

Elvira is wondering how many students were sitting at the front table when she wrote her first note. Unfortunately, she is not sure what order the middle three Post-It Notes were recorded in since they got stuck together in random order. She is wondering if it matters.

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2. Does it matter which order the notes were recorded in? Determine how many students were originally sitting at the front table based on the sequence of notes that appears above. Then rearrange the middle three notes in a different order and determine what the new order implies about the number of students seated at the front table at the beginning.
3. Here are three different equations that could be written based on a particular sequence of notes. Examine each equation, and then list the order of the five notes that is represented by each equation. Find the solution for each equation.

- $\frac{2(x+4)}{3} = 12$

- $2\left(\frac{x}{3} + 4\right) = 12$

- $\frac{2x+4}{3} = 12$



1.5 Cafeteria Actions and Reactions – Teacher Notes

A Develop Understanding Task

Purpose: In this task students will develop insights into how to extend the process of solving equations—which they have examined previously for one- or two-step equations—to work with multistep equations. The process of solving an equation consists of writing a sequence of equivalent equations until the value(s) that make each of the equations in the sequence true becomes evident. Each equation in the sequence of equivalent equations is obtained by operating on the expressions on each side of the previous equation in the same way, such as multiplying both sides of the equation by the same amount, or adding the same amount to both sides of the equation. This property of equality is often referred to as “keeping the equation in balance.” Our goal in each step of the equation solving process is to make the next equivalent equation contain fewer operations than the previous one by “un-doing” one operation at a time. When there are multiple operations involved in an equation, the order in which to “un-do” the operations can be somewhat problematic. This task examines ways to determine the sequence of “un-do-it” steps by using the structure of the equation.

Core Standards Focus:

A.REI.1 Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

Related Standards: A.REI.3

Launch (Whole Class):

Read the initial story context about Elvira, the cafeteria manager, and the sequence of events that led to “twelve new trays in each of three serving lines” and challenge students to “un-do” the actions that got her to this situation to see if they can answer Elvira’s question of “how many trays were in each carton?” Give students a few minutes to work individually or with a partner to analyze this situation, then have a student share his or her thinking.

Record the steps of the explanation of how to find the number of trays in a carton for use in a few minutes:

- Since there are now twelve trays in each of three serving lines, there must have been 36 trays before Elvira divided them up.
- Since 24 students removed trays after lunch period started, there must have been $36+24=60$ trays that were unloaded.
- Since the 60 trays came from 4 cartons, there must have been 15 trays in each carton.



Now propose that the story of Elvira’s “actions” could have been represented by the following sequence of equivalent equations, and have students connect each equation in the sequence to the appropriate action:

Let $x = 15$	This represents the number of trays in each carton.
$4x = 60$	This would represent the number of trays unloaded from four cartons.
$4x - 24 = 36$	This would represent the remaining trays after 24 students passed through the line.
$\frac{4x - 24}{3} = 12$	This would represent the number of trays in each of the three lines.

This last equation represents a multi-step equation. Have students pretend that we do not know the solution for x . Have them discuss with a partner how they could look at this equation and “see” the steps listed on the board for “un-doing” the story, as represented by the numbers and operations in this equation. Have students share what they have noticed, then have them work on the second situation with Elvira and the Post-It Notes.

Explore (Small Group):

Encourage students to do the same thing with the 5 Post-It Notes that they did with the serving trays scenario. That is, they should write out the steps of reasoning that would help them work backwards to the solution. Have them then change the order of the middle three Post-It Notes and solve the situation again. Ask, did the order matter?

Listen for how students are making decisions about which order the notes were arranged in for each of the three different equations listed in problem 3.

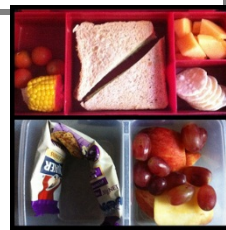
Discuss (Whole Class):

The discussion should focus on question 3 and how students can recognize the order of events that got to “still 12 students seated at the front table.” Once they can see how the sequence of events unfolded, they should be able to determine how to reverse the sequence of events. It may be necessary to write out the list of events and “un-do-it” explanations for each problem, similar to what was done in the launch.

Aligned Ready, Set, Go: Getting Ready 1.5



Name: _____

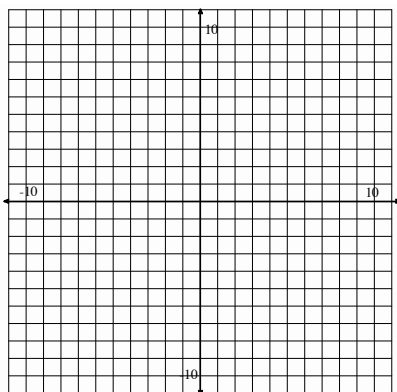
Getting Ready **5****Ready, Set, Go!****Ready**

Topic: Solutions to an equation

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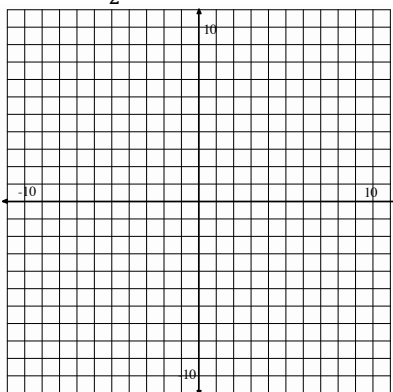
Graph the following equations using the coordinate graph, and then say if the given point is a solution to the equation.

1. $y = 5x - 2$



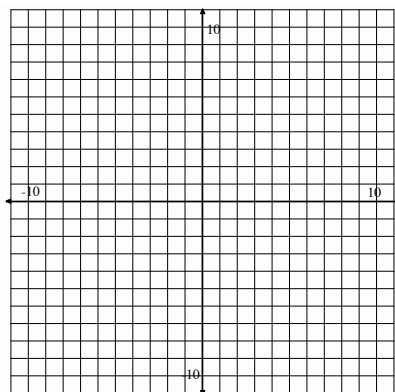
Point: (1, 3) Yes / No

2. $y = -\frac{1}{2}x + 8$



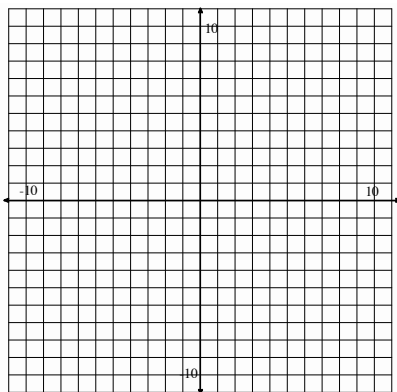
Point: (0, 4) Yes / No

3. $y = x + 4$



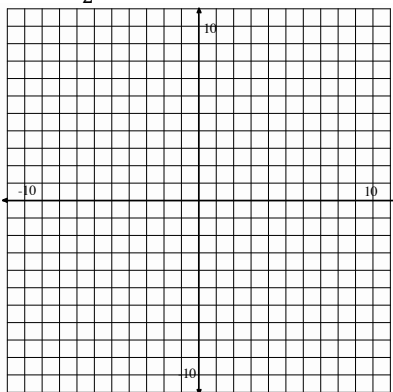
Point: (-2, 2) Yes / No

4. $y = x + 2$



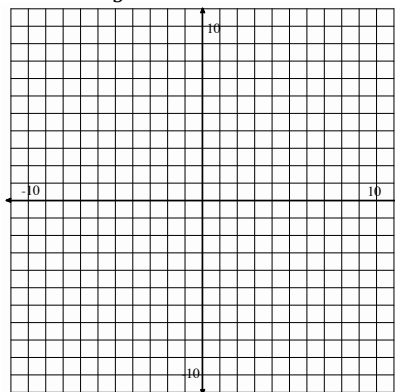
Point: (1, 3) Yes / No

5. $y = \frac{5}{2}x - 7$



Point: (2, -2) Yes / No

6. $y = -\frac{4}{3}x$



Point: (4, -6) Yes / No

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Set

7. The solution to an equation is $n = -5$. The equation has parentheses on at least one side of the equation and has variables on both sides of the equation. What could the equation be?

8. Create a two-step equation that is true by expanding the given solution using properties of equality. Draw a model to represent your expanded equation.

a. $x = 3$

$m = -2$

$a = 0$

9. Without solving, determine if the two expressions are equivalent. Explain your reasoning.

a. $14 - (3a + 2) = 14 - 3a - 2$

b. $4a - 10 = 2(2a - 5)$

10. Without solving, determine if these two equations have the same solution.

$3(x - 5) = 35$ and $3x - 5 = 35$. Why or why not?

11. Which of the following expressions are equivalent?

$\frac{4t-10}{2}$

$\frac{4t}{2} - 10$

$2t - 10$

$4t - 5$



Go

Check whether the given number is a solution to the corresponding equation.

12. $a = -3$; $4a + 3 = -9$

13. $x = \frac{4}{3}$; $\frac{3}{4}x + \frac{1}{2} = \frac{3}{2}$

14. $y = 2$; $2.5y - 10.0 = -0.5$

15. $z = -5$; $2(5 - 2z) = 20 - 2(z - 1)$

Need Help? Check out these related videos:

<http://www.khanacademy.org/math/algebra/solving-linear-equations/v/solving-equations-1>

<http://www.khanacademy.org/math/algebra/linear-equations-and-inequalitie/v/graphing-a-line-in-slope-intercept-form>

<http://www.youtube.com/watch?v=WxzpisUh0AU>

<http://patrickjmt.com/an-intro-to-solving-linear-equations-what-does-it-mean-to-be-a-solution/>

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1.6 Elvira's Equations

A Solidify Understanding Task

(Note: This task refers to the same set of variables as used in *Serving Up Symbols*)



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Elvira, the cafeteria manager, has written the following equation to describe a cafeteria relationship that seems meaningful to her. She has introduced a new variable A to describe this relationship.

$$A = \frac{S}{CP}$$

1. What does A represent in terms of the school and the cafeteria?
2. Using what you know about manipulating equations, solve this equation for S . Your solution will be of the form $S = \text{an expression written in terms of the variables } A, C \text{ and } P$.
3. Does your expression for S make sense in terms of the meanings of the other variables? Explain why or why not.
4. Now solve the above equation for C and explain why the solution makes sense in terms of the variables.

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Here is another one of Elvira's equations.

$$T_s = \frac{S(N_e + N_s + N_b)}{i}$$

5. What does T_s represent in terms of the school and the cafeteria?

(Hint: Elvira was really clever here. She recognized that the expression $N_e + N_s + N_b$ counted the number of *items/lunch*. She also noticed that since S represented the number of students that eat lunch each day, S also counted the number of *lunches* served. Using these new units, what would the product $S(N_e + N_s + N_b)$ mean? What would the quotient named T_s mean?)

6. Using what you know about manipulating equations, solve this equation for S .

7. Does your expression for S make sense in terms of the meanings of the other variables? Explain why or why not.

8. Now solve the above equation for N_e and explain why the solution makes sense in terms of the variables.



1.6 Elvira's Equations – Teacher Notes

A Solidify Understanding Task

Purpose: The purpose of this task is to apply the equation solving process developed in the previous task to solving literal equations and formulas. Working with literal equations solidifies the notion that operations have to be “un-done” in an appropriate order by doing the inverse operation to both sides of the equation. This task also solidifies the meaning of expressions by attending to the units associated with each of the variables.

Core Standards Focus:

A.REI.3 Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

Related Standards: A.REI.1, N.Q.1

Launch (Whole Class):

Work through problems 1-4 together as a class, then have students work on problems 5-8 with a partner. In problem 1, students need to pay attention to the units on the variables and the meaning of the parts of the expression obtained after operating with these variables. For example, multiplying C classes/lunch period times P lunch periods/day gives an expression in the denominator of the fraction that represents $classes/day$. Dividing S students/day by CP classes/day gives the average number of $students/class$ as the meaning for the variable A .

Solving for S in question 2 leads to $S=ACP$. To verify that this makes sense, we can determine the units on S (which should be $students/day$) by determining the units on the product:

$$(A \text{ students/class}) \times (C \text{ classes/lunch period}) \times (P \text{ lunch periods/day})$$

The unit on the product is also $students/day$.

Do a similar analysis for $C = \frac{S}{AP}$.

Explore (Small Group):

As students work on questions 5-8 listen for the meaning they are giving to the new variable T_S .

Note: While S literally represents the number of students who buy lunch each day, it can be reassigned as representing the number of *lunches* served in a day. This is a typical issue when modeling real-world situations—identifying the meaning of the variables in a useful, yet consistent way. With this interpretation of S , as well as some carefully assigned units for the other variables,

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students should be able to determine that T_S represents the total number of minutes it takes to serve all student lunch. That is, $S \text{ lunches} \times (N_e + N_s + N_b) \text{ items/lunch} \div i \text{ items/minute}$ yields $T_S \text{ minutes}$. If students are getting bogged down making sense of this variable, suggest that they work on questions 6 and 8, solving for a particular variable, and defer the discussion of the meaning of the variables until the whole class discussion. The expression for the right side of the equation was chosen to be particularly complex in order to raise issues about solving equations, rather than interpreting the meaning of the units.

Discuss (Whole Class):

Begin by focusing on how to solve Elvira's second equation for S and for N_e . Students might find more than one correct way to write the solution for N_e depending on whether they distributed S or not. Discuss and clarify all proposed solutions.

If some students have been able to interpret the meaning of T_S as *minutes* required to serve all of the lunches, have them present. If not, work out with students how the units on T_S can be interpreted as *minutes*. This should assist students in checking the units for consistent meaning in the expressions they write for S and N_e .

Aligned Ready, Set, Go: Getting Ready 1.6



Name: _____

Getting Ready **6****Ready, Set, Go!**

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Ready

Topic: Solve literal equations

Solve each equation for x . Justify each step.

1. $ax = d$

2. $b + cx = d$

3. $ab + cx = d$

Set

Topic: Solve literal equations or writing linear equations in slope-intercept form

Rearrange the following equations to solve for y (slope-intercept form).

4. $4x + y = 3$

5. $2y = 6x + 9$

6. $5x - 2y = 10$

7. $3x + 6y = 25$

8. $x - 8y = 12$

9. $3x - 7y = 20$

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Go

Topic: Create and solve equations for real world problems

Create an equation that describes each of the situations below, then solve.

10. The cost of a birthday party at Classic Boon is \$200 plus \$4 per person. The cost for Fletcher's party came to \$324. How many people came to his party?

11. A cell phone company charges \$55 per month for unlimited minutes plus \$0.25 per text sent. If the charges to Dayne's cell phone for last month came to \$100, how many texts did Aly send?

12. Aly has baked an apple pie and wants to sell it in her bakery. She is going to cut it into 12 slices and sell them individually. She wants to sell it for three times the cost of making it. The ingredients cost \$8.50, and she allowed \$1.25 to cover the cost of electricity to bake it. Find the values for each of the following questions:

- a) What is the amount Aly will charge for each slice of pie?
- b) What is the total amount she will gross if she sells the entire pie?
- c) What will be the profit if she sells the entire pie?

Need Help? Check out these related videos:

Solve and justify two step equations using properties of equality <http://www.youtube.com/watch?v=WXzpisUh0AU>

Rearrange equations to highlight a variable: solve literal equations

<http://www.khanacademy.org/math/algebra/solving-linear-equations/v/example-of-solving-for-a-variable>

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1.7 Solving Equations, Literally

A Practice Understanding Task



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Solve each of the following equations for x :

1. $\frac{3x+2}{5} = 7$

2. $\frac{3x+2y}{5} = 7$

3. $\frac{4x}{3} - 5 = 11$

4. $\frac{4x}{3} - 5y = 11$

5. $\frac{2}{5}(x+3) = 6$

6. $\frac{2}{5}(x+y) = 6$

7. $2(3x+4) = 4x+12$

8. $2(3x+4y) = 4x+12y$

Write a verbal description for each step of the equation solving process used to solve the following equations for x . Your description should include statements about how you know what to do next. For example, you might write, "First I _____, because _____."

9. $\frac{ax+b}{c} - d = e$

10. $r \cdot \sqrt{\frac{mx}{n}} + s = t$

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1.7 Solving Equations, Literally – Teacher Notes

A Practice Understanding Task

Purpose: This task provides practice for solving linear equations in one variable, solving linear equations in two variables for one of its variables, and solving literal equations. The process for solving multivariable equations for one of its variables becomes more apparent when juxtaposed with similarly-formatted equations in one variable. The only difference in the solution process is the ability to carry out numerical computations to simplify the expressions in the one-variable equations.

Core Standards Focus:

A.REI.1 Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

A.REI.3 Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

Related Standards:

Launch (Whole Class):

Encourage students to note the similarities in their work on the pairs of problems in questions 1-8. Also point out that they are to write detailed explanations of their solution strategy on problems 9 and 10. One way to facilitate this would be to have students fold a piece of paper in half lengthwise. On the left side of the paper they write out their algebra steps, and on the right side they write out their justifications.

Explore (Small Group):

Monitor students while working on these problems and offer appropriate feedback, as necessary. Some of the problems have alternative strategies, such as #5 where you can distribute the $\frac{2}{5}$ first, or multiply both sides of the equations by $\frac{5}{2}$ first. Help students recognize the difference between changing the form of an expression on one side of an equation, vs. writing an equivalent equation by applying the same operation to both sides.

If students are having difficulties with #9 or #10, have them write a related equation in which they replace all letters with numbers except for the x . See if they can solve the related equation for x and if that work can help them solve the original literal equation. Problem 10 involves a square root in order to emphasize that one of the key issues in solving an equation is to “un-do” an operation by

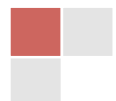


applying the inverse operation to both sides. Help students think about how that would play out in problem 10. That is, how might they “un-do” a square root?

Discuss (Whole Class):

Have students present their solution process for any problems that may have been difficult for a number of students. You might also want to have students critique each other’s explanations on problems 9 and 10 by having students exchange papers. They should fold their partner’s paper in half, so that only the right side with the written explanation is showing. On a separate sheet of paper they should write-out the algebra steps they would take to solve each problem, based only on the wording of their partners’ explanation. They should discuss any explanations that are unclear with their partner.

Aligned Ready, Set, Go: Getting Ready 1.7



Name:

Getting Ready | 1.7

Ready, Set, Go!

Ready

Topic: Inequalities



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Use the inequality $4 < 6$ to complete each row in the table.

Apply each operation to the original inequality $4 < 6$	Result	Is the inequality true or false?
1. Add 4 to both sides		
2. Add -4 to both sides		
3. Subtract 10 from both sides		
4. Multiply both sides by 4		
5. Divide both sides by 2		
6. Multiply both sides by -3		
7. Divide both sides by -2		

In general, what operations, when performed on an inequality, *reverse* the inequality?

Set

Topic: Solve literal equations

Solve for the indicated variable.

8. Solve the following equation to isolate F : $C = \frac{5}{9}(F - 32)$
9. For $V = \frac{1}{3}\pi r^2 h$, rewrite the formula to isolate the variable h .
10. The area formula of a regular polygon is $A = \frac{1}{2}Pa$. The variable a represents the apothem and P represents the perimeter of the polygon. Rewrite the equation to highlight the value of the perimeter, P .

11. The equation $y = mx + b$ is the equation of a line. Isolate the variable m .

12. The equation $y = mx + b$ is the equation of a line. Isolate the variable x .

13. $Ax + By = C$ is the standard form for a line. Isolate the equation for x .

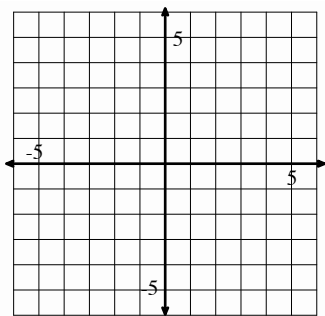
14. $Ax + By = C$ is the standard form for a line. Isolate the equation for y .

Go

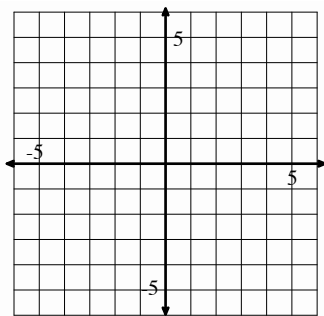
Topic: Solve systems of linear equations

Solve linear equations and pairs of simultaneous linear equations (simple, with a graph only) by graphing both lines and finding where they intersect. Justify the solution numerically.

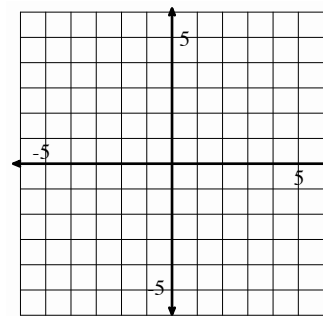
15. $y = x + 3$ and $y = -x + 3$



16. $y = 3x - 6$ and $y = -x + 6$



17. $2x = 4$ and $y = -3$



Need Help? Check out these related videos:

<http://www.khanacademy.org/math/algebra/solving-linear-inequalities/v/equations-and-inequalities>

<http://www.khanacademy.org/math/algebra/solving-linear-equations/v/solving-for-a-variable>

<http://www.khanacademy.org/math/algebra/systems-of-eq-and-ineq/v/solving-linear-systems-by-graphing>

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1.8 Cafeteria Conundrums

A Solidify Understanding Task

Between serving and preparing delicious school lunches, our cafeteria manager, Elvira, is busy analyzing the business of running the cafeteria. We previously saw the symbols for some of the things that she measured. Now she plans to use those symbols. Help Elvira to consider the pressing questions of the lunch room.



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Symbol	Meaning
S	Number of students that buy lunch in the cafeteria each day
S_m	Number of students who have passed through a line in m minutes
C	Number of classes per lunch period
P	Number of lunch periods per day
B	Number of boys that buy lunch each day
G	Number of girls that buy lunch each day
F	Number of food servers in the cafeteria
T	Total number of food items in one lunch (Each entrée, side dish, or beverage counts as 1 item.)
M	Number of minutes passed since the beginning of the lunch period
N_e	Number of entrees in each lunch
N_s	Number of side dishes in each lunch
N_b	Number of beverages in each lunch
C_e	Cost of each entrée
C_s	Cost of each side dish
C_b	Cost of each beverage
L	Number of lines in the cafeteria
W	The number of food workers (servers) per line
i	Average number of food items that a worker can serve each minute (Each entrée, side dish, or beverage counts as 1 item.)
H	Number of hours each food worker works each day
P_L	Price per lunch



Write equations or inequalities to express some of the conditions that Elvira sees in the cafeteria.

1. Each lunch can have no more than 4 side dishes.
2. More boys eat school lunch than girls.
3. There can be no more than 7 food items in each lunch.
4. In each lunch, there are 3 more side dishes than entrees and twice as many beverages as entrees. Write an inequality in **one variable** that shows that the total number of food items in a lunch cannot be more than 7.
5. The cost of food in the lunch is the total of the cost of the entrée, the side dishes, and the beverages. Write an inequality that shows that the cost of the food in the lunch must be less than \$1.50.
6. To meet district guidelines, the total price of a lunch must be more than \$2.25, but less than \$3.50.
7. Elvira knows that the number of lines that she can open in the cafeteria depends on how many food servers she has in the cafeteria each day and how many workers are needed in each line. Write an inequality that shows this relationship.
8. Food workers are paid \$11.50 per hour. Elvira can't spend more than \$500 per day on employees. Write an inequality that relates the number of food workers to the amount spent each day on employees.
9. Elvira knows that the money she gets from selling lunches has to be greater than her costs.
 - a. Write an expression for the cost of employees each day
 - b. Write an expression for the cost of food each day
 - c. Write an expression that shows that the total cost of food and employees each day must be less than the amount she brings in from selling lunches.

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1.8 Cafeteria Conundrums

A Solidify Understanding Task

Purpose: This is the first task in a series of three that works with the ideas of inequalities. Most students have been introduced to solving inequalities in their earlier experiences in mathematics. Each of the inequalities tasks in the unit emphasis reasoning with variables and symbols, and the use of inequalities in a context. This task extends the work that students have previously done with symbols and equations to setting up inequalities. The Ready, Set, Go homework that coordinates with the task reviews and practices skills for solving inequalities.

Core Standards Focus:

A.REI.1 Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution.
a. Construct a viable argument to justify a solution method.
b. Solve equations and inequalities in one variable.

A.REI.3 Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

Mathematics I Note: *Extend earlier work with solving linear equations to solving linear inequalities in one variable and to solving literal equations that are linear in the variable being solved for.*

Launch (Whole Class):

Remind students of the work that they have done with previous task that have been set in the school cafeteria, starting with Serving Up Symbols. This task uses all the same symbols that they are already familiar with. You may also wish to review the use of each of the inequality symbols, \neq , \leq , $<$, \geq , and $>$ before getting into the task. Start by asking students to work problem 1 on their own. Ask students which symbol they used for the phrase “no more than” and how they know it was \leq rather than $<$. Tell student that in this task they will need to consider both the variable to use and the correct symbol to describe the relationship.

Explore (Small Group or Pairs):

Ask students to complete the task. Circulate around the room, initially watching for their work with problems 3 and 4. These are related problems with #4 requiring substitution into the inequality that students write for #3. The context in problem 6 suggests writing a compound inequality, which students may not have seen previously. They may choose to write two inequalities for this problem, which would be an interesting topic for the class discussion. Throughout the course of the exploration, watch for problems that are generating controversy, challenge, or interesting thinking so that they can be highlighted during the class discussion.



Discuss (Whole Class):

Start the discussion with any problem that has been identified during the exploration phase. Then turn the attention to problem 9. Ask a different student to explain each part, a, b, and c. Ask students why the total cost of food and employees each day must be less than the amount she brings in from selling lunches. What would it mean if we wrote an equation, rather than an inequality for these two expressions?

Aligned Ready, Set, Go: Getting Ready 1.8



Name:

Getting Ready **8****Ready, Set, Go!**

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Ready

Topic: Solving equations

Jesse was asked to solve an algebra problem. She submitted the following solution

$$4(x + 3) = 1$$

$$4x + 3 = 1$$

$$4x = -2$$

$$x = -2$$

1. Is Jesse's solution correct?
2. If it is correct, justify each step of her solution.
3. If it is incorrect, correct her solution, and explain to Jesse what she did wrong.

Set

Topic: Creating and solving real world problems

4. Jade is stranded downtown with only \$10 to get home. Taxis cost \$0.75 per mile, but there is an additional \$2.35 hire charge. Write a formula and use it to calculate how many miles she can travel with her money.

5. Jasmin's Dad is planning a surprise birthday party for her. He will hire a bouncy castle, and will provide party food for all the guests. The bouncy castle costs \$150 for the afternoon, and the food will cost \$3 per person. Andrew, Jasmin's Dad, has a budget of \$300. Write an equation and use it to determine the maximum number of guests he can invite.

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6. Jane is baking cookies for a large party. She has a recipe that will make one batch of two dozen cookies, and she decides to make five batches. To make five batches, she finds that she will need 12.5 cups of flour and 15 eggs. Write an equation to describe each of the following situations. Then solve the problem.
- How many cookies will she make in all?
 - How many cups of flour go into one batch?
 - How many eggs go into one batch?
 - If Jane only has a dozen eggs on hand, how many more does she need to make five batches?
 - If she doesn't go out to get more eggs, how many batches can she make? How many cookies will that be?

Go

Topic: Solve systems of equations

Solve the following systems of equations by graphing. You may use a graphing calculator.

7. Mary's car has broken down and it will cost her \$1200 to get it fixed—or, for \$4500, she can buy a new, more efficient car instead. Her present car uses about \$2000 worth of gas per year, while gas for the new car would cost about \$1500 per year. After how many years would the total cost of fixing the car equal the total cost of replacing it?
8. Juan is considering two cell phone plans. The first company charges \$120 for the phone and \$30 per month for the calling plan that Juan wants. The second company charges \$40 for the same phone but charges \$45 per month for the calling plan that Juan wants. After how many months would the total cost of the two plans be the same?
9. A tortoise and hare decide to race 30 feet. The hare, being much faster, decides to give the tortoise a 20 foot head start. The tortoise runs at 0.5 feet/sec and the hare runs at 5.5 feet per second. How long until the hare catches the tortoise?

Need Help? Check out these related videos:

<http://www.youtube.com/watch?v=EWcllbr8Hqs&feature=related>

http://www.youtube.com/watch?v=ldYGiXSHa_Q

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1.9 Greater Than?

A Solidify Understanding Task

For each situation you are given a mathematical statement and two expressions beneath it.

1. Decide which of the two expressions is greater, if the expressions are equal, or if the relationship cannot be determined from the statement.
2. Write an equation or inequality that shows your answer.
3. Explain why your answer is correct.

Watch out—this gets tricky!

Example:

Statement: $x = 8$

Which is greater? $x + 5$ or $3x + 2$

Answer: $3x + 2 > x + 5$ because if $x = 8$, $3x + 2 = 26$, $x + 5 = 13$ and $26 > 13$.

Try it yourself:

1. Statement: $y < x$
Which is greater? $x - y$ or $y - x$
2. Statement: $2x - 3 > 7$
Which is greater? 5 or x
3. Statement: $10 - 2x < 6$
Which is greater? x or 2
4. Statement: $4x = 0$
Which is greater? 1 or x
5. Statement: $a > 0$, $b < 0$
Which is greater? ab or $\frac{a}{b}$



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6. Statement: n is an integer
Which is greater? n or $-n$

7. Statement:
Which is greater? 1 or yz



8. Statement: Use the number line in #7 and $x < w < y$
Which is greater? w or $-y$

9. Statement: $0 < x < 10$ and $0 < y < 12$
Which is greater? x or y

10. Statement: $3^{n+2} = 27$
Which is greater? n or 3

11. Statement: $5 > 4$
Which is greater? $5x$ or $4x$

12. Statement $x > y$
Which is greater? $x + a$ or $y + a$

13. Statement: $5 > 4$
Which is greater? $\frac{5}{x}$ or $\frac{4}{x}$

14. Statement: $x > y$ and $a > b$
Which is greater? $x - a$ or $y - b$

15. Statement: $x > 0, y > 0, \frac{x}{y} > 2$
Which is greater? $2y$ or x



1.9 Greater Than? – Teacher Notes

A Solidify Understanding Task

Purpose: The purpose of this task is to challenge students to think deeply about inequality relationships and to understand the properties of inequalities. Each of the problems in the require reasoning about numbers, including negative numbers and fractions, and thinking mathematically about the various possibilities in the given problem situation.

Core Standards Focus:

A.REI.1 Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution.
a. Construct a viable argument to justify a solution method.
b. Solve equations and inequalities in one variable.

A.REI.3 Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

Mathematics I Note: *Extend earlier work with solving linear equations to solving linear inequalities in one variable and to solving literal equations that are linear in the variable being solved for.*

Launch (Whole Class):

Explain to students that this task is a big logic puzzle. All of the problems require thinking about all the different possibilities to decide which expression is greater. There are some that cannot be determined from the information given. You may choose not to tell students this in advance so that they have an opportunity to wrestle with the ideas and to justify their position. Start by asking students to read the example given. To confirm the instructions, ask how they see the 3 required parts of the explanation in the answer. Next, refer students to problem #1. Give them a few minutes to answer and write their own explanation. Ask the class for their answers and explanation and model how to write an answer with a complete explanation. You may also want to model thinking about possible value for x and y , like: “If x is a negative number, then y must also be a negative number because it is less than x .”

Explore (Small Group or Pairs): Monitor students as they work. Encourage them to think about the various possibilities for x and y in each case. Be sure that their written explanations adequately communicate their logic. Watch for problems that generate disagreement or difficulty for the class discussion. Also look for students’ explanations that demonstrate sound mathematical logic or good communication to be highlighted in the discussion. If you notice a common misconception occurring during the exploration, plan to raise it as an issue in the discussion.

Discuss (Whole Class): Start the discussion with problems 11-15. Ask previously-selected students to give their explanations for each of these problems. Highlight for the class that these three problems are asking them to justify the properties of inequalities. Write each of the properties of inequalities (addition, subtraction, multiplication, and division), and ask students to



state them in their own words. After going through each of these, turn the discussion to any misconceptions or provocative problems that were selected during the exploration phase.

Aligned Ready, Set, Go Homework: Getting Ready 1.9



Name: _____

Getting Ready **1.9****Ready, Set, Go!**

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Ready

Topic: Solve inequalities, create and solve equations.

Solve the following inequalities for x.

1. $2x - 9 < 3$

2. $4x - 3 < 13$

3. $6x - 4 < 26$

4. $3x - 5 \geq 10$

Create and solve the equations for the following problems.

- Virginia's Painting Service charges \$10 per job and \$0.20 per square foot. If Virginia earns \$50 for painting one job, how many square feet did she paint at the job?
- Renting the ice-skating rink for Dayne's birthday party costs \$200 plus \$4 per person. If the cost was \$324, how many people were at Dayne's birthday party?

Set

Topic: Solve inequalities

Solve each inequality. Write the solution as an inequality.

7. $x + 15 < 12$

8. $x - 4 \geq 13$

9. $9x > -\frac{3}{4}$

10. $3x - 7 \geq 3(x - 7)$

11. $x - 12 \geq 80$

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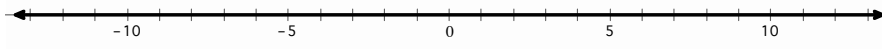
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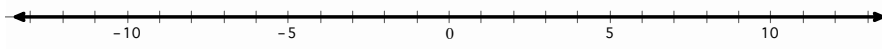


Solve each inequality and graph the solution on the number line.

12. $x - 2 \leq 1$

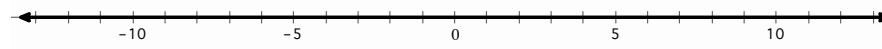


13. $x - 8 > -20$

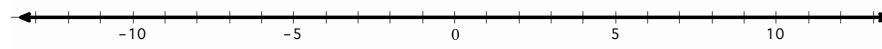


Solve each inequality. Write the solution as an inequality and graph it.

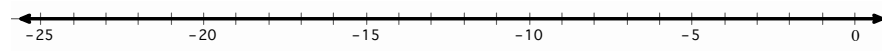
14. $3x \leq 6$



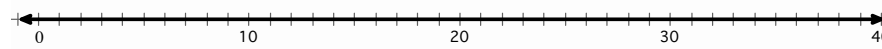
15. $\frac{x}{5} > -\frac{3}{10}$



16. $-10x > 150$



17. $\frac{x}{7} \geq -5$



Solve each multi-step inequality.

18. $x - 5 > 2x + 3$

19. $\frac{3(x-4)}{12} \leq \frac{2x}{3}$

20. $2(x - 3) \leq 3x - 2$



Go

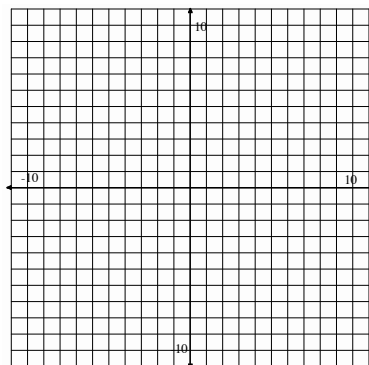
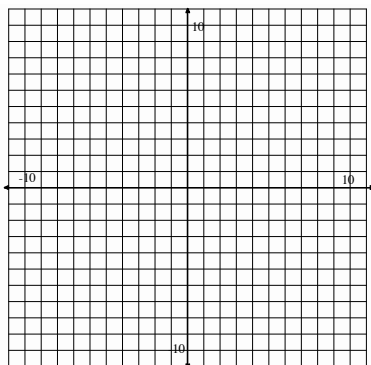
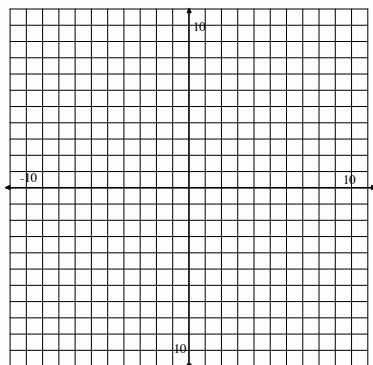
Topic: Solve systems of linear equations

Solve linear equations and pairs of simultaneous linear equations (simple, with a graph only). Justify the solution numerically.

$$21. \begin{cases} y = -x + 5 \\ -x + y = 1 \end{cases}$$

$$22. \begin{cases} x + 2y = 8 \\ 5x + 2y = 0 \end{cases}$$

$$23. \begin{cases} 3x + 2y = 12 \\ 4x - y = 5 \end{cases}$$



Need Help? Check out these related videos:

<http://www.khanacademy.org/math/algebra/solving-linear-inequalities/v/equations-and-inequalities>

<http://www.khanacademy.org/math/algebra/solving-linear-equations/v/solving-for-a-variable>

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1.10 Taking Sides

A Practice Task

Joaquin and Serena work together productively in their math class. They both contribute their thinking and when they disagree, they both give their reasons and decide together who is right. In their math class right now, they are working on inequalities. Recently they had a discussion that went something like this:



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Joaquin: The problem says that “6 less than a number is greater than 4.” I think that we should just follow the words and write $6 - x > 4$.

Serena: I don’t think that works because if x is 20 and you do 6 less than that you get $20 - 6 = 14$. I think we should write $x - 6 > 4$.

Joaquin: Oh, you’re right. Then it makes sense that the solution will be $x > 10$, which means we can choose any number greater than 10.

The situations below are a few more of the disagreements and questions that Joaquin and Serena have. Your job is to decide how to answer their questions, decide who is right, and give a mathematical explanation of your reasoning.

1. Joaquin and Serena are assigned to graph the inequality $x \geq -7$.
Joaquin thinks the graph should have an open dot -7 .
Serena thinks the graph should have a closed dot at -7 .
Explain who is correct and why.
2. Joaquin and Serena are looking at the problem $3x + 1 > 0$.
Serena says that the inequality is always true because multiplying a number by three and then adding one to it makes the number greater than zero.
Is she right? Explain why or why not.
3. The word problem that Joaquin and Serena are working on says, “4 greater than x ”.
Joaquin says that they should write: $4 > x$.
Serena says they should write: $x + 4$.
Explain who is correct and why.



4. Joaquin is thinking hard about equations and inequalities and comes up with this idea:
If $45 + 47 = t$, then $t = 45 + 47$.
So, if $45 + 47 < t$, then $t < 45 + 47$.
Is he right? Explain why or why not.
5. Joaquin's question in #4 made Serena think about other similarities and differences in equations and inequalities. Serena wonders about the equation $-\frac{x}{3} = 4$ and the inequality $-\frac{x}{3} > 4$. Explain to Serena ways that solving these two problems are alike and ways that they are different. How are the solutions to the problems alike and different?
6. Joaquin solved $-15q \leq 135$ by adding 15 to each side of the inequality. Serena said that he was wrong. Who do you think is right and why?
- Joaquin's solution was $q \leq 150$. He checked his work by substituting 150 for q in the original inequality. Does this prove that Joaquin is right? Explain why or why not.
- Joaquin is still skeptical and believes that he is right. Find a number that satisfies his solution but does not satisfy the original inequality.
7. Serena is working is checking her work with Joaquin and finds that they disagree on a problem. Here's what Serena wrote:
- $$3x + 3 \leq -2x + 5$$
- $$3x \leq -2x + 2$$
- $$x \leq 2$$
- Is she right? Explain why or why not?
8. Joaquin and Serena are having trouble solving $-4(3m - 1) \geq 2(m + 3)$.
Explain how they should solve the inequality, showing all the necessary steps and identifying the properties you would use.



9. Joaquin and Serena know that some equations are true for any value of the variable and some equations are never true, no matter what value is chosen for the variable. They are wondering about inequalities. What could you tell them about the following inequalities? Do they have solutions? What are they? How would you graph their solutions on a number line?
- $4s + 6 \geq 6 + 4s$
 - $3r + 5 > 3r - 2$
 - $4(n + 1) < 4n - 3$
10. The partners are given the literal inequality $ax + b > c$ to solve for x . Joaquin says that he will solve it just like an equation. Serena says that he needs to be careful because if a is a negative number, the solution will be different. What do you say? What are the solutions for the inequality?



1.10 Taking Sides – Teacher Notes

A Practice Task

Purpose: The purpose of this task is to practice the reasoning and solving of inequalities. Many common misconceptions and mistakes made when solving inequalities are addressed in the task. Students are asked to think about the differences and similarities in solving inequalities versus solving equations, including that most inequalities produce a range of solutions, that the inequality sign must be turned when multiplying or dividing by a negative number, and that the reflexive property holds only for equations.

Core Standards:

A.REI.1 Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution.
a. Construct a viable argument to justify a solution method.
b. Solve equations and inequalities in one variable.

A.REI.3 Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

Mathematics I Note: *Extend earlier work with solving linear equations to solving linear inequalities in one variable and to solving literal equations that are linear in the variable being solved for.*

Launch (Whole Class):

Hand out the worksheet and go over the scenario given about Joaquin and Serena. Ask a student to demonstrate Serena’s argument that changed Joaquin’s mind. Before moving to problem #1, tell students that they should work on a separate piece of paper or in their journals, as there is not adequate room on the handout for their explanations. Start with #1, giving students about 3 minutes to answer the question individually, writing their best explanation in complete sentences. Ask a student to read their explanation and then model a thorough answer on the board. The explanation should be something like:

The inequality $x \geq -7$ should be graphed with a closed dot on -7 and all points to the right of -7 filled in. This is because the symbol \geq means greater than or equal to, so -7 is a solution to the inequality. The closed dot on -7 shows that the number is included in the solution set. An open dot would indicate that -7 is not a solution.

Next, ask the class to think about #2. Give students a few minutes to talk to their neighbor about their reasoning and then ask them to write individually for a few minutes. While they are working, circulate through the room to find an exemplar to use with the class. It is important that students are first considering the logic of why Serena believes the inequality to always be true. Then, students should recognize that she is only considering nonnegative numbers. Be sure that both



parts of the argument are discussed to model the thinking process that will be required throughout the task and also what a complete answer will look like.

Explore (Small Group):

Let student work on the remainder of the task as you monitor their thinking. Throughout the task, students will be challenged to consider whether the strategies that they have learned for equations will apply to inequalities. If you find that some groups are spending excessive time on a problem, redirect their focus to problems 4, 5, 7, and 8, which will be the focus of the whole group discussion. Identify a group to present one of each of these problems.

Discuss (Whole Group):

Start the discussion with the presentation of problem #4. Be sure that the group identifies that if the two sides of an equation are switched, the equation remains true. Their explanation should also include the idea that if the sides of an inequality are switched, then the inequality sign must be turned. Ask the group to demonstrate this thinking by substituting numbers into the inequality for x . Remind students that this often comes up because the solutions to inequalities are conventionally written with the variable on the left side of the inequality. So, an expression like $4 < x$ is routinely converted to $x > 4$.

Next, move the discussion to #5. Again, students are asked to consider the difference between solving an equation and solving an inequality. The explanation from the group should include the idea that the steps in solving the equation and the inequality are the same. The only difference is that the inequality sign must be turned when multiplying by -3 . Press students to explain why that rule holds, rather than simply stating the rule.

The explanation of #7 should include showing all the proper steps in the solution of the inequality. As students demonstrate the problem, they will see that Serena did not properly add $2x$ to both sides of the inequality. Ask students why this inequality seemed to be solved exactly like an equation, but other inequalities do not.

Close the discussion with question #8. Emphasize the reasons for each step and compare the properties of inequalities with the properties of equations.

Aligned Ready, Set, Go: Getting Ready 1.10



Name: _____

Getting Ready | 10

Ready, Set, Go!

Ready

Topic: Solving equations and inequalities



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1. The local amusement park sells summer memberships for \$50 each. Normal admission to the park costs \$25; admission for members costs \$15.
 - a. If Darren wants to spend no more than \$100 on trips to the amusement park this summer, how many visits can he make if he buys a membership with part of that money?
 - b. How many visits can he make if he does not?
 - c. If he increases his budget to \$160, how many visits can he make as a member?
 - d. How many can he make as a non-member?

2. Jae just took a math test with 20 questions, each worth an equal number of points. The test is worth 100 points total.
 - a. Write an equation relating the number of questions Jae got right to the total score he will get on the test.
 - b. If a score of 70 points earns a grade of *C-*, how many questions would Jae need to get right to get a *C-* on the test?
 - c. If a score of 83 points earns a grade of *B*, how many questions would Jae need to get right to get a *B* on the test?
 - d. Suppose Jae got a score of 60% and then was allowed to retake the test. On the retake, he got all the questions right that he got right the first time, and also got half the questions right that he got wrong the first time. What percent did Jae get right on the retake?

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Set

Topic: Solve and justify one variable inequalities

Solve each inequality, justifying each step you use.

3.

$x - 5 < 35$	Justification

4.

$x + 68 \geq 75$	Justification

5.

$2x - 4 \leq 10$	Justification

6.

$5 - 4x \leq 17$	Justification

7.

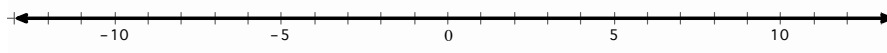
$\frac{x}{-3} > -\frac{10}{9}$	Justification

8.

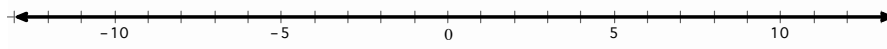
$2(x - 3) \leq 3x - 2$	Justification

Solve each inequality and graph the solution on the number line.

9. $x - 8 > -20$



10. $x + 11 > 13$



Solve each multi-step inequality.

11. $4x + 3 < -1$

12. $4 - 6x \leq 2(2x + 3)$

13. $5(4x + 3) \geq 9(x - 2) - x$

14. $\frac{2}{3}x - \frac{1}{2}(4x - 1) \geq x + 2(x - 3)$

Topic: Solve literal equations

15. Solve the following equation to isolate C : $F = \frac{9}{5}C + 32$

16. For $V = \frac{1}{3}\pi r^2 h$, rewrite the formula to isolate the variable r .

17. The area formula of a regular polygon is $A = \frac{1}{2}Pa$. The variable a represents the apothem and P represents the perimeter of the polygon. Rewrite the equation to highlight the value of the apothem, a .

18. The equation $y = mx + b$ is the equation of a line. Isolate the variable b

19. The equation for the circumference c of a circle with radius r is $c = 2\pi r$. Solve the equation for the radius, r .

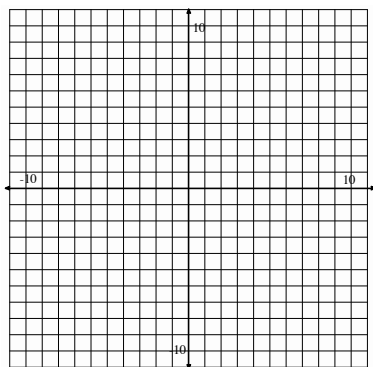
20. The equation for the area of a circle A with diameter d is $A = \pi \frac{d^2}{4}$. Solve the equation to isolate the diameter, d .

Go

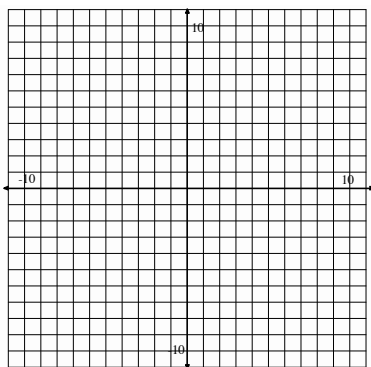
Topic: Solve systems of equations

Solve linear equations and pairs of simultaneous linear equations (simple, with a graph only). Justify the solution numerically.

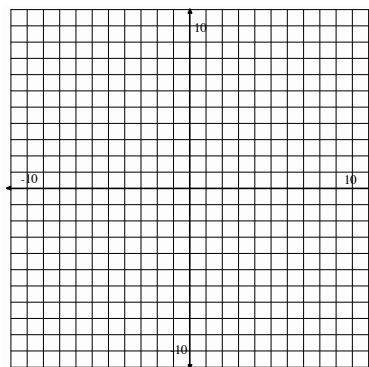
$$21. \begin{cases} y = 2x + 5 \\ -x + y = 1 \end{cases}$$



$$22. \begin{cases} 3x - 2y = 16 \\ x + 2y = 0 \end{cases}$$



$$23. \begin{cases} 3x + 2y = 11 \\ 4x - y = 10 \end{cases}$$



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