

Secondary One Mathematics: An Integrated Approach

Module 8

Modeling Data

By

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Module 8 – Modeling Data

Classroom Task: 8.1 Texting By the Numbers- A Solidify Understanding Task

Use context to describe data distribution and compare statistical representations (S.ID.1, S.ID.3)

Ready, Set, Go Homework: Modeling Data 8.1

Classroom Task: 8.2 Data Distributions – A Solidify/Practice Understanding Task

Describe data distributions and compare two or more data sets (S.ID.1, S.ID.3)

Ready, Set, Go Homework: Modeling Data 8.2

Classroom Task: 8.3 After School Activity – A Solidify Understanding Task

Interpret two way frequency tables (S.ID.5)

Ready, Set, Go Homework: Modeling Data 8.3

Classroom Task: 8.4 Relative Frequency– A Solidify Understanding Task

Use context to interpret and write conditional statements using relative frequency tables (S.ID.5)

Ready, Set, Go Homework: Modeling Data 8.4

Classroom Task: 8.5 Connect the Dots– A Develop Understanding Task

Develop an understanding of the value of the correlation co-efficient (S.ID.8)

Ready, Set, Go Homework: Modeling Data 8.5

Classroom Task: 8.6 Making More \$ – A Solidify Understanding Task

Estimate correlation and lines of best fit. Compare to the calculated results of linear regressions and correlation the co-efficient (S.ID.7, S.ID.8)

Ready, Set, Go Homework: Modeling Data 8.6

Classroom Task: 8.7 Getting Schooled – A Solidify Understanding Task

Use linear models of data and interpret the slope and intercept of regression lines with various units (S.ID.6, S.ID.7, S.ID.8)

Ready, Set, Go Homework: Modeling Data 8.7

Classroom Task: 8.8 Rocking the Residuals – A Develop Understanding Task

Use residual plots to analyze the strength of a linear model for data (S.ID.6)

Ready, Set, Go Homework: Modeling Data 8.8



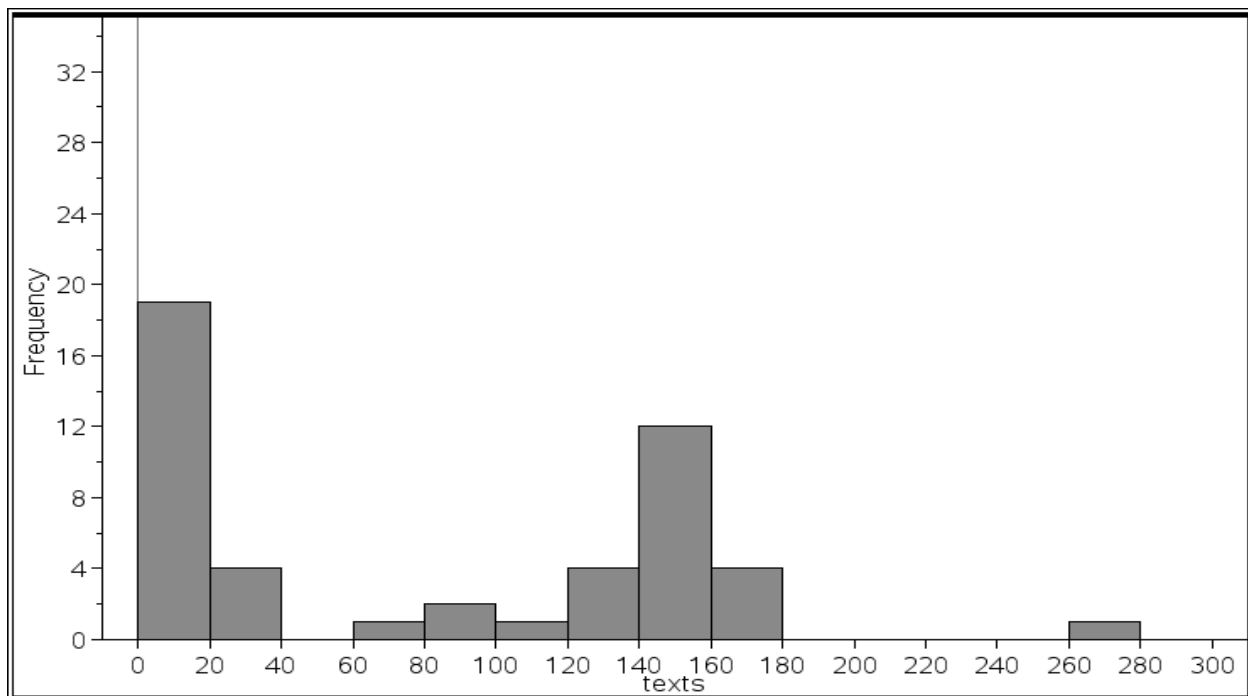
8.1 Texting by the Numbers

A Solidify Understanding Task

Technology changes quickly and yet has a large impact on our lives.

Recently, Rachel was busy chatting with her friends via text message when her mom was trying to also have a conversation with her. Afterward, they had a discussion about what is an appropriate amount of texts to send each day. Since they could not agree, they decided to collect data on the number of texts people send on any given day. They each asked 24 of their friends the following question: “What is the average number of texts you SEND each day?” The data and histogram representing all 48 responses are below:

{150, 5.5, 6, 5, 3, 10, 150, 15, 20, 15, 6, 5, 3, 6, 0, 5, 12, 25, 16, 35, 5, 2, 13, 5, 130, 145, 155, 150, 162, 80, 140, 150, 165, 138, 175, 275, 85, 137, 110, 143, 138, 142, 164, 70, 150, 36, 150, 150}

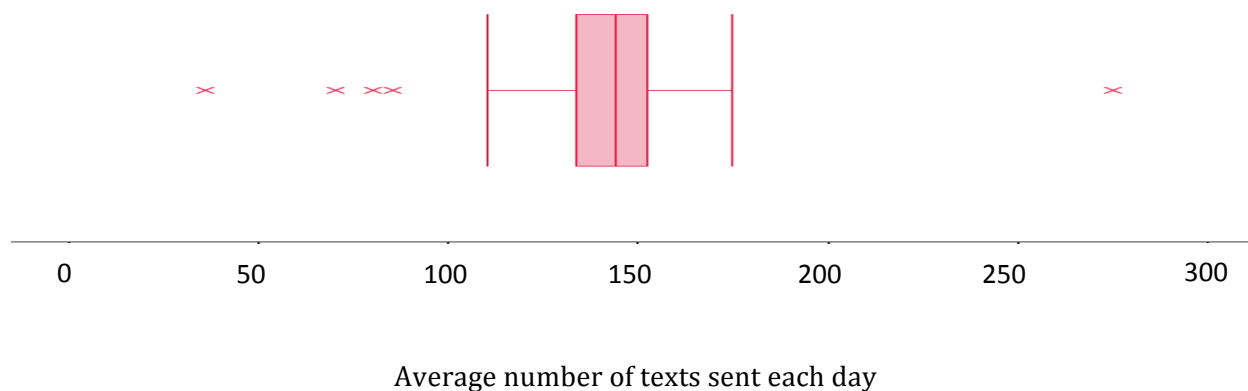


Part I: What information can you conclude based on the histogram above?

Represent the same data by creating a box plot below.

Describe the pros and cons of each representation (histogram and box plot). In other words, what information does each representation highlight? What information does each representation hide or obscure?

Part II: Prior to talking about the data with her mom, Rachel had created a box plot using her own data she collected and it looked quite different than when they combined their data.



Describe the data Rachel collected from her friends. What does this information tell you?

What do you think is a reasonable number of texts Rachel can send per day?

Rachel wants to continue sending her normal number of texts (average of 100 per day) and her mom would like her to decrease this by half. Present an argument for each side, using mathematics to justify each person's request.

Name:

Modeling Data | 8.1

Ready, Set, Go!

<http://www.flickr.com/photos/garryknight/740038>

Ready

Topic: Measures of central tendency

Sam's test scores for the term were 60, 89, 83, 99, 95, and 60.

1. Suppose that Sam's teacher decided to base the term grade on the mean.
 - a. What grade would Sam receive?
 - b. Do you think this is a fair grade? Explain your reasoning.

2. Suppose that Sam's teacher decided to base the term grade on his median score.
 - a. What grade would Sam receive?
 - b. Do you think this is a fair grade? Explain your reasoning.

3. Suppose that Sam's teacher decided to base the term grade on the mode score.
 - a. What grade would Sam receive?
 - b. Do you think this is a fair grade? Explain your reasoning.

4. Aiden's test scores for the same term were 30, 70, 90, 90, 91, and 99. Which measure of central tendency would Aiden want his teacher to base his grade on? Justify your thinking.

5. Most teachers base grades on the mean. Do you think this is a fair way to assign grades? Why or why not?

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Name:

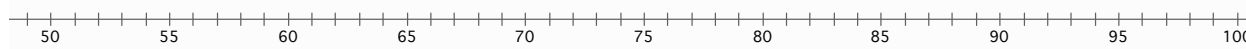
Modeling Data | 8.1

Set

Topic: Examining data distributions in a box-and-whisker plot

60, 64, 68, 68, 72, 76, 76, 80, 80, 80, 84, 84, 84, 84, 88, 88, 88, 92, 92, 96, 96, 96, 96, 96, 96, 96, 100, 100

6. Make a box-and-whisker plot for the following test scores.



7a. How much of the data is represented by the box?

b. How much is represented by each whisker?

8. What does the graph tell you about student success on the test?

Go

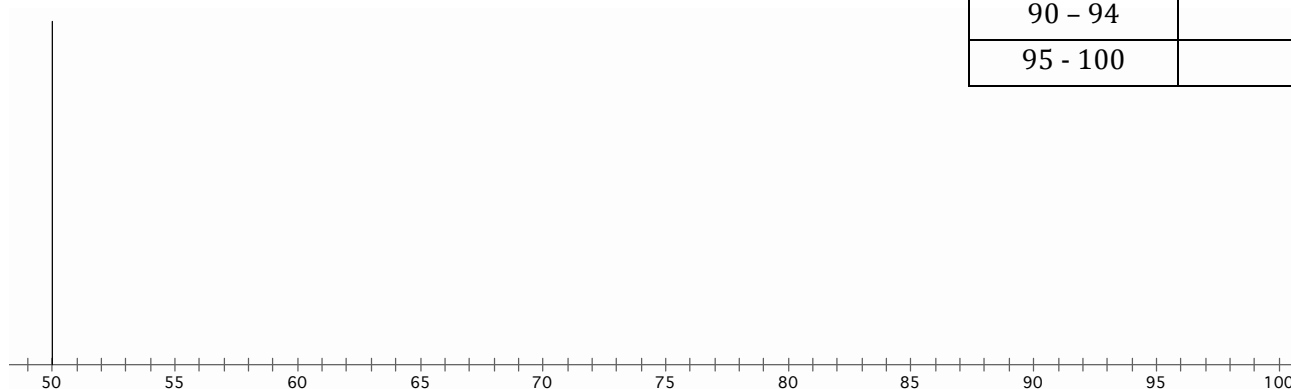
Topic: Drawing histograms.

Use the data from the SET section to answer the following questions

9. Make a frequency table with intervals. Use an interval of 5.

10. Make a histogram of the data using your intervals of 5.

Score	Frequency
60 - 64	
65 - 69	
70 - 74	
75 - 79	
80 - 84	
85 - 89	
90 - 94	
95 - 100	



Need Help? Check out these related videos:

http://www.khanacademy.org/math/statistics/e/mean_median_and_mode
<http://www.khanacademy.org/math/algebra/ck12-algebra-1/v/box-and-whisker-plot>
<http://www.khanacademy.org/math/algebra/ck12-algebra-1/v/histograms>

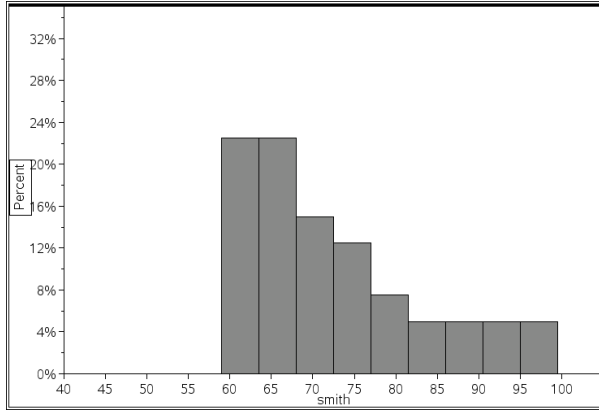
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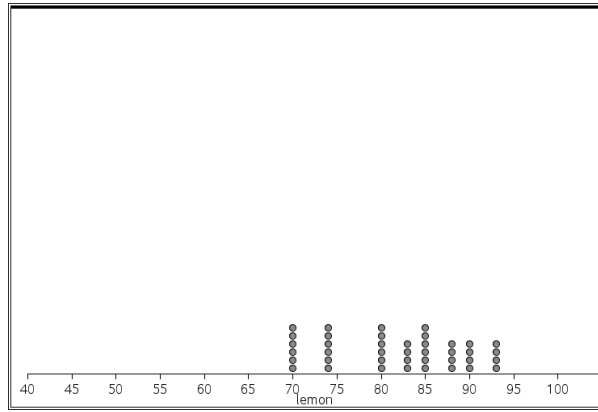
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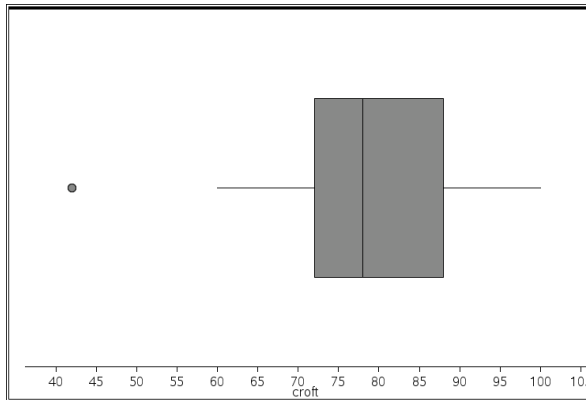
Data set I: Smith's class



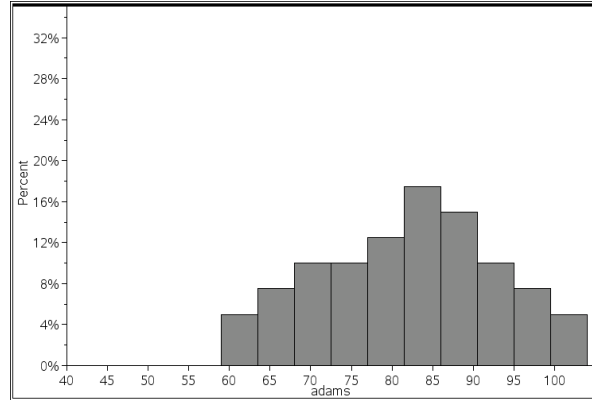
Data set II: Lemon's class



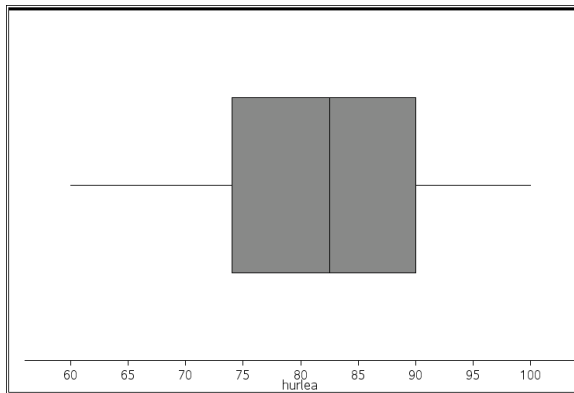
Data set III: Croft's Class



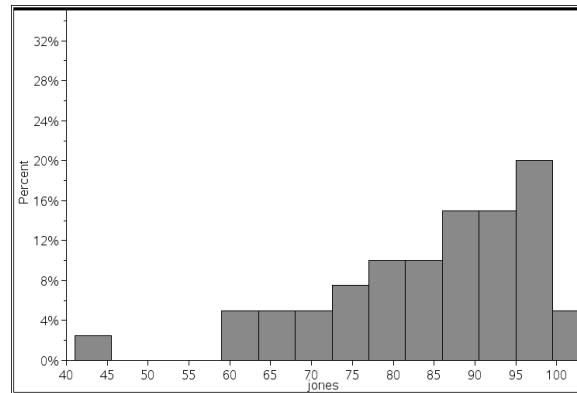
Data set IV: Adam's Class



Data set V: Hurlea's class



Data set VI: Jones' class



Name: _____

Modeling Data | 8.2

Ready, Set, Go!

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Ready

Topic: Sequences in statistics

In problems 1 – 4 you are to select the best answer based on the given data. Below your chosen answer is a confidence scale. Circle the statement that best describes your confidence in the correctness of the answer you chose.

1. Data: 1, 2, 4, 8, 16, 32, _____? The next number in the list will be: _____
 a. larger than 32 b. positive c. exactly 64 d. about 63.89

I am certain I am correct. **I am a little unsure.** **I had no idea so I guessed.**

What about the data made you feel the way you did about the answer you marked?

2. Data: 47, -13, -8, 9, -23, 14, _____? The next number in the list will be: _____
 a. positive b. negative c. less than 100 d. less than -100

I am certain I am correct. **I am a little unsure.** **I had no idea so I guessed.**

What about the data made you feel the way you did about the answer you marked?

3. Data: -10, $\frac{3}{4}$, 38, -10, $\frac{1}{2}$, -81, -10, $\frac{1}{4}$, 93, -10, _____? The next number in the list will be: _____
 a. more than 93 b. negative c. a fraction d. a whole number

I am certain I am correct. **I am a little unsure.** **I had no idea so I guessed.**

What about the data made you feel the way you did about the answer you marked?

4. Data: 50, -43, 36, -29, 22, -15, _____? The next number in the list will be: _____
 a. odd b. less than 9 c. two-digits d. greater than -15

I am certain I am correct. **I am a little unsure.** **I had no idea so I guessed.**

What about the data made you feel the way you did about the answer you marked?

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Name:

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Set

Topic: Drawing histograms.

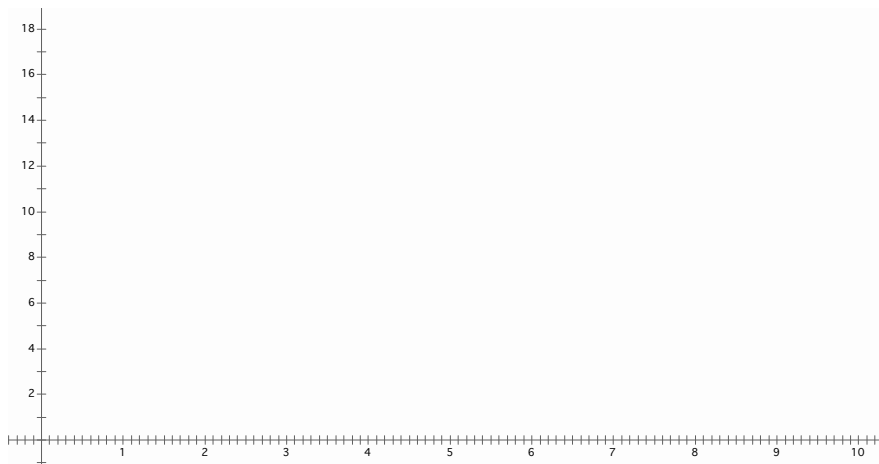
Mr. Austin gave a ten-point quiz to his 9th grade math classes. A total of 50 students took the quiz. Mr. Austin scored the quizzes and listed the scores alphabetically as follows.

1 st Period Math	2 nd Period Math	3 rd Period Math
6, 4, 5, 7, 5,	4, 5, 8, 6, 8,	9, 8, 10, 5, 9,
9, 5, 4, 6, 6,	9, 5, 8, 5, 1,	7, 8, 9, 8, 5,
8, 5, 7, 5, 8,	5, 5, 7, 5, 7	8, 10, 8, 8, 5
1, 8, 7, 10, 9		

5. Use the ALL of the quiz data to make a frequency table with intervals. Use an interval of 2.

Score	Frequency
0 - 1	
2 - 3	
4 - 5	
6 - 7	
8 - 10	

6. Use your frequency table to make a histogram for the data



7. Describe the data distribution of the histogram you created. Include words such as: *mode*, *skewed*, *outlier*, *normal*, *symmetric*, *center*, and *spread*, if they apply.

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Name:

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Go

8. What percent of 97 is 11? 9. What percent of 88 is 132?
10. What percent of 84 is 9? 11. What percent of 88.6 is 70?
12. What is 270% of 60? 13. What is 84% of 25?

Need Help? Check out these related videos:

<http://www.khanacademy.org/math/algebra/ck12-algebra-1/v/histograms>

<http://www.khanacademy.org/math/statistics/v/ck12-org-normal-distribution-problems--qualitative-sense-of-normal-distributions>

<http://stattrek.com/statistics/two-way-table.aspx>

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8.3 After School Activity

A Develop Understanding Task



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Part I

Rashid is in charge of determining the upcoming after school activity. To determine the type of activity, Rashid asked several students whether they prefer to have a dance or play a game of soccer. As Rashid collected preferences, he organized the data in the following two-way frequency table:

	Girls	Boys	Total
Soccer	14	40	54
Dance	46	6	52
Total	60	46	106

Rashid is feeling unsure of the activity he should choose based on the data he has collected and is asking for help. To better understand how the data is displayed, it is useful to know that the outer numbers, located in the margins of the table, represent the total frequency for each row or column of corresponding values and are called *marginal frequencies*. Values that are part of the 'inner' body of the table are created by the intersection of information from the column and the row and they are called the *joint frequencies*. Using the data in the table, construct a viable argument and explain to Rashid which after school event he should choose.

Part II: Two way frequency tables allow us to organize categorical data in order to draw conclusions. For each set of data below, create a frequency table. When each frequency table is complete, write three sentences about observations of the data, including any trends or associations in the data.

Data set 1: There are 45 total students who like to read books. Of those students, 12 of them like non-fiction and the rest like fiction. Four girls like non-fiction. Twenty boys like fiction.

	Fiction	Nonfiction	Total
Boys			
Girls			
Total			

Observation 1:

Observation 2:

Observation 3:

Data set 2: 35 seventh graders and 41 eighth graders completed a survey about the amount of time they spend on homework each night. 50 students said they spent more than an hour. 12 eighth graders said they spend less than an hour each night.

			Total
More than one hour			
Less than one hour			
Total			

Observation 1:

Observation 2:

Observation 3:

Name:

Modeling Data | 8.3

Ready, Set, Go!

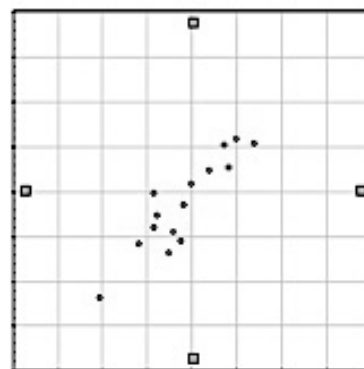
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Ready

Topic: Interpreting data from a scatter plot

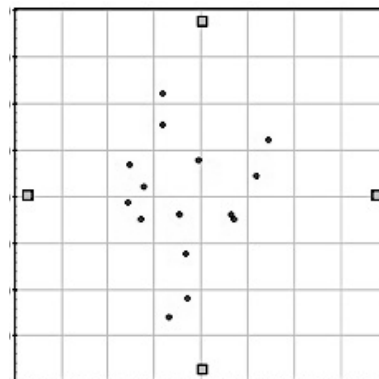
1. The scatter plot compares shoe size and height in adult males. Based on the graph, do you think there is a relationship between a man's shoe size and his height?

Explain your answer.



2. The scatter plot compares left-handedness to birth weight. Based on the graph, do you think being left-handed is related to a person's birth weight?

Explain your answer.



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Name:

Modeling Data | 8.3

Set

Topic: Two-way frequency tables.

Here is the data from Mr. Austin's ten-point quiz. Students needed to score a 6 or better to pass the quiz.

1 st Period Math	2 nd Period Math	3 rd Period Math
6, 4, 3, 7, 5,	3, 3, 8, 6, 6,	9, 8, 10, 5, 9,
9, 5, 4, 6, 6,	9, 5, 8, 5, 3,	7, 8, 9, 8, 3,
8, 5, 7, 3, 6,	5, 5, 7, 5, 7	8, 10, 8, 7, 5
2, 8, 7, 10, 9		

3. Make a two-way frequency table showing how many students passed the quiz and how many failed in each class.

	1 st Period	2 nd Period	3 rd Period	Total
Passed				
Failed				
Total				

4. Use a colored pencil to lightly shade the cells containing the *joint frequency* numbers in the table. The un-shaded numbers are the *marginal frequencies*. (Use these terms to answer the following questions.)

5. If Mr. Austin wanted to see how many students in all 3 classes combined passed the quiz, where would he look?

6. If Mr. Austin wanted to write a ratio of the number of passing students compared to the number of failing students for each class, where would he find the numbers he would need to do this?

7. Make a two-way frequency table that gives the *relative frequencies* of the quiz scores for each class.

	1 st Period	2 nd Period	3 rd Period	Total
Passed				
Failed				
Total				

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Name:

Modeling Data | 8.3

Go

8. Sophie surveyed all of the 6th grade students at Reagan Elementary School to find out which TV Network was their favorite. She thought that it would be important to know whether the respondent was a boy or a girl so she recorded her information this way.

Animal Planet	Cartoon Network	Disney	Nickelodeon
GGBBBB BGBBBG GGBB BBBB	BBBBBBB BBGGBBBG BGBGGBGG	GGGGGBBBBB GBGBGG BBBGBGG GGBBBGGGG	BBBBGGGGGGG GGGGGGB GGGBGGGGGGGG BGGGGGGG

Sophie planned to use her data to answer the following questions:

- I. Are there more girls or boys in the 6th grade?
- II. Which network was the boys' favorite?
- III. Was there a network that was favored by more than 50% of one gender?

But when she looked at her chart, she realized that the data wasn't telling her what she wanted to know. Her teacher suggested that her data would be easier to analyze if she could organize it into a two-way frequency chart. Help Sophie out by putting the frequencies into the correct cells.

<i>Favorite TV Networks</i>	<i>Girls</i>	<i>Boys</i>	<i>Totals</i>
Animal Planet			
Cartoon Network			
Disney			
Nickelodeon			
<i>Totals</i>			

Now that Sophie has her data organized, use the two-way frequency chart to answer her 3 questions.

- a. Are there more girls or boys in the 6th grade?
- b. Which network was the boys' favorite?
- c. Was there a network that was favored by more than 50% of one gender?

Need Help? Check out these related links:

<http://stattrek.com/statistics/two-way-table.aspx>

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8.4 Relative Frequency

A Solidify Understanding Task

Rachel is thinking about the data she and her mom collected for the average number of texts a person sends each day and started thinking that perhaps a two-way table of the data they collected would help convince her mom that she does not send an excessive amount of texts for a teenager. The table separates each data point by age (teenager and adult) and by the average number of texts sent (more than 100 per day or less than 100 per day).

	Average is more than 100 texts sent per day	Average is less than 100 texts sent per day	Total
Teenager	20	4	24
Adult	2	22	24
Total	22	26	48

Write two observation statements of this two way table.

To further provide evidence, Rachel decided to do some research. She found that only 43% of people with phones send over 100 texts per day. She was disappointed that the data did not support her case and confused because it did not seem to match what she found in her survey. What questions do these statistic raise for you? What data should Rachel look for to support her case?

After looking more closely at the data, Rachel found other percentages within the same data that seemed more accurate with the data she collected from her teenage friends. How might Rachel use the data in the two way table to find percentages that would be useful for her case?

Part II: Once Rachel realized there are a lot of ways to look at a set of data in a two way table, she was self-motivated to learn about *relative frequency tables* and conditional frequencies. When the data is written as a percent, this is called a *relative frequency table*. In this situation, the 'inner' values represent a percent and are called **conditional frequencies**. The conditional values in a *relative frequency table* can be calculated as percentages of one of the following:

- the whole table (relative frequency of table)
- the rows (relative frequency of rows)
- the columns (relative frequency of column)

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Since Rachel wants to emphasize that a person's age makes a difference in the number of texts sent, the first thing she decided to do is focus on the ROW of values so she could write conditional statements about the number of texts a person is likely to send based on their age. This is called a *relative frequency of row* table. Fill in the percentage of teenagers for each of the conditional frequencies in the highlighted row below:

Row →

	Average is more than 100 texts sent per day	Average is less than 100 texts sent per day	Total
Teenager	20	4	24
% of teenagers	__ %	__%	100%
% of Adults	2 8%	22 92%	24 100%
% of People	22 46%	26 54%	48 100%

Since the PERCENTAGES created focus on ROW values, all conditional observations are specific to the information in the row. Complete the following sentence for the *relative frequency of row*:

Of all teenagers in the survey, _____ % average more than 100 texts per day.

Write another statement based on the *relative frequency of row*:

Below is the *relative frequency of column* using the same data. This time, all of the percentages are calculated using the data in the column.

	Average is more than 100 texts sent per day	Average is less than 100 texts sent per day	Total
Teenagers	20 91%	4 15%	24 50%
Adults	2 9%	22 85%	24 50%
Total	22 100%	26 100%	48 100%

Write two conditional statements using the *relative frequency of column*.



This data represents the *relative frequency of whole table*:

	Average is more than 100 texts sent per day	Average is less than 100 texts sent per day	Total
% of Teenagers	20 42%	4 8%	24 50%
% of Adults	2 4%	22 46%	24 50%
% of Total	22 46%	26 54%	48 100%

Create two conditional distribution statements for the *relative frequency of whole table*

How do *relative frequency tables* impact the way you look at data in two way tables?



Name:

Modeling Data | 8.4

Ready, Set, Go!



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Ready

Topic: Linear functions and relationships

Write the explicit linear function for the given information below.

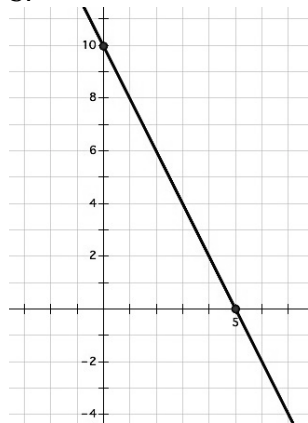
1. $(3, 7)$ $(5, 13)$

2. Mike earns \$11.50 an hour

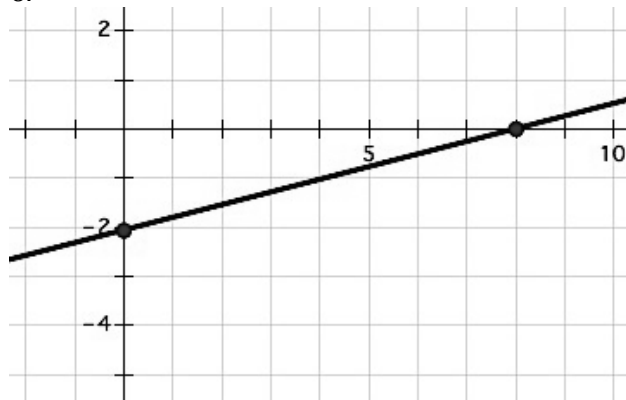
3. $(-5, -2)$ $(1, 10)$

4. $(-2, 12)$ $(6, 8)$

5.



6.



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Name:

Modeling Data | 8.4

Set

Topic: Relative Frequency Tables

For each two-way table below, create the indicated relative frequency table and also provide two observations with regard to the data.

7. This table represents survey results from a sample of students regarding mode of transportation to and from school.

	Walk	Bike	Car Pool	Bus	Total
Boys	37	47	27	122	233
Girls	38	22	53	79	192
Total	75	69	80	201	425

Create the *relative frequency of row table*. Then provide two observation statements.

	Walk	Bike	Car Pool	Bus	Total
Boys					
Girls					
Total	100%	100%	100%	100%	100%

8. The two-way table contains survey data regarding family size and pet ownership.

	No Pets	Own one Pet	More than one pet	Total
Families of 4 or less	35	52	85	172
Families of 5 or more	15	18	10	43
Total	50	70	95	215

Create the *relative frequency of column table*. Then provide two observation statements.

	No Pets	Own one Pet	More than one pet	Total
Families of 4 or less				100%
Families of 5 or more				100%
Total				100%

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9. The two-way table below contains survey data about boys and girls shoes.

	Athletic shoes	Boots	Dress Shoe	Total
Girls	21	35	60	116
Boys	50	16	10	76
Total	71	51	70	192

Create the *relative frequency of whole table*. Then provide two observation statements.

	Athletic shoes	Boots	Dress Shoe	Total
Girls				
Boys				
Total				100%

Go

Topic: One variable statistical measures and comparisons

For each set of data determine the mean, median, mode and range. Then create either a box-and-whisker plot or a histogram.

10. 23, 24, 25, 20, 25, 29, 24, 25, 30

11. 20, 24, 10, 35, 25, 29, 24, 25, 33

12. How do the data sets in problems 10 and 11 compare to one another?

13. 2, 3, 4, 5, 3, 4, 7, 4, 4

14. 1, 1, 3, 5, 5, 10, 5, 1, 14

15. How do the data sets in problems 13 and 14 compare to one another?

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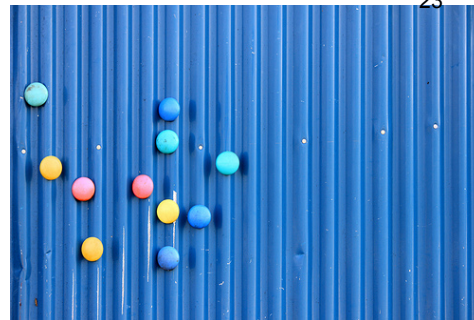
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8.5 Connect the Dots

A Develop Understanding Task



- For each set of data:
 - Graph on a scatter plot.
 - Use technology (graphing calculator or computer) to calculate the correlation coefficient.

Set A

2	2.3	3.3	3.7	4.2	4.6	4.5	5	5.5	5.7	6.1	6.4
1	1.5	2.5	1.9	2.8	3.2	4.5	3.7	1.7	4.8	2.7	2.3

Set B

2	2.3	3.3	3.7	4.2	4.6	4.5	5	5.5	5.7	6.1	6.4
1	1.5	2.5	1.9	2.8	3.2	4.5	3.7	4	4.8	5	4.6

Set C

2	2.3	3.3	3.7	4.2	4.6	4.5	5	5.5	5.7	6.1	6.4
4.7	4.9	4.2	3.9	3.5	3.2	3.1	2.6	3.2	2.1	1.3	0.8

Set D

2	2.3	3.3	3.7	4.2	4.6	4.5	5	5.5	5.7	6.1	6.4
4.7	4.9	3.6	3.9	2.1	4.5	3.1	1.7	3.7	2.1	1.3	1.8

Set E

2	2.3	3.3	3.7	4.2	4.6	4.5	5	5.5	5.7	6.1	6.4
4.7	4	4.2	3.9	2.8	3.2	4.5	3.7	3.2	4.8	5	4.4

Set F

2	2.3	3.3	3.7	4.2	4.6	4.5	5
1.8	2.22	3.62	4.18	4.88	5.44	5.3	6

Set G

2	2.3	3.3	3.7	4.2	4.6	4.5	5
4.4	4.01	2.71	2.19	1.54	1.02	1.15	0.5

- Put the scatter plots in order based upon the correlation coefficients.
- Compare each scatter plot with its correlation coefficient. What patterns do you see?

4. Use the data in Set A as a starting point. Keeping the same x -values, modify the y -values to obtain a correlation coefficient as close to 0.75 as you can.

Record your data here.

2	2.3	3.3	3.7	4.2	4.6	4.5	5	5.5	5.7	6.1	6.4

What did you have to do with the data to get a greater correlation coefficient?

5. This time, again start with the data in Set A. Keep the same x -values, but this time, modify the y values to obtain a correlation coefficient as close to 0.25 as you can.

Record your data here.

2	2.3	3.3	3.7	4.2	4.6	4.5	5	5.5	5.7	6.1	6.4

What did you have to do with the data to get a correlation coefficient that is closer to 0?

6. One more time: start with the data in Set A. Keep the same x -values, modify the y -values to obtain a correlation coefficient as close to -0.5 as you can.

Record your data here.

2	2.3	3.3	3.7	4.2	4.6	4.5	5	5.5	5.7	6.1	6.4

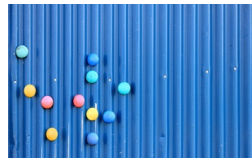
What did you have to do with the data to get a correlation coefficient that is negative?

7. What aspects of the data does the correlation coefficient appear to describe?

Name: _____

Modeling Data | 8.5

Ready, Set, Go!



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Ready

Topic: Estimating the line of best fit

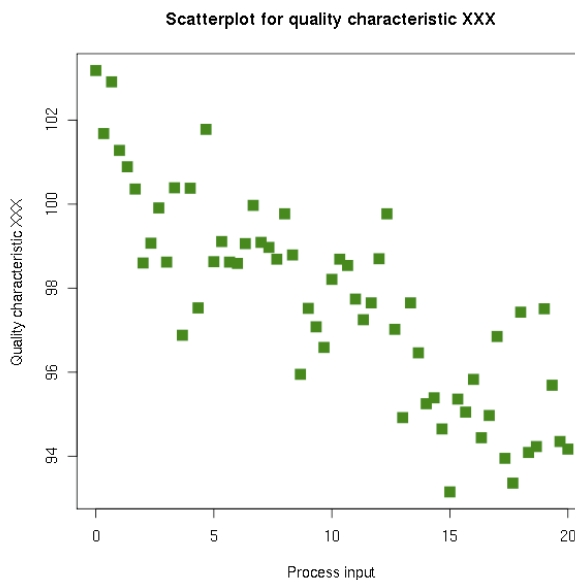
Examine the scatterplot below. Imagine that you drew a straight line through the general pattern of the points, keeping as close as possible to all points with as many points above the line as below.

1. Predict a possible y-intercept and slope for that line.

a. y-intercept: _____

b. slope: _____

2. Sketch the line that you imagined for question #1 and write an equation for that line.

© 2012 http://en.wikipedia.org/wiki/File:Scatter_diagram_for_quality_characteristic_XXX.svg

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Name: _____

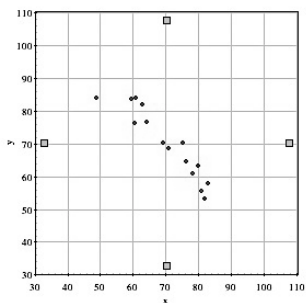
Modeling Data | 8.5

Set

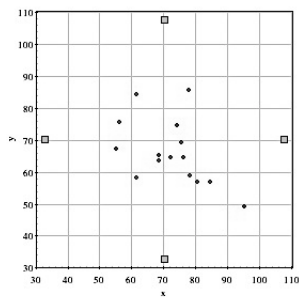
Topic: Estimating the correlation coefficient

Match the scatterplot with its correlation coefficient.

___ 3.



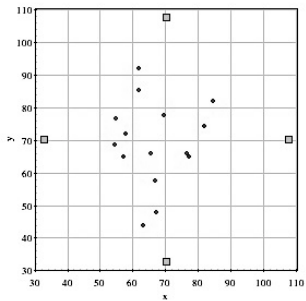
___ 4.



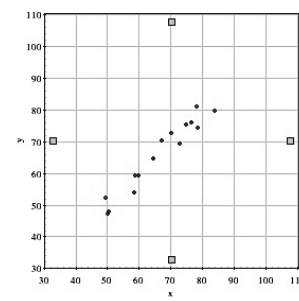
Possible
Correlation Coefficients

- a. 0.05
- b. 0.97
- c. -0.94
- d. -0.49
- e. 0.68

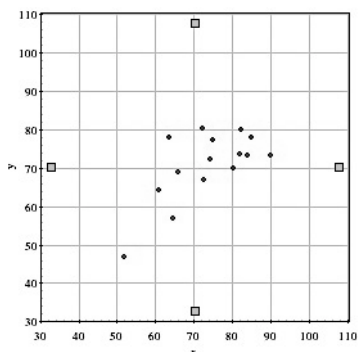
___ 5.



___ 6.



___ 7.



Name:

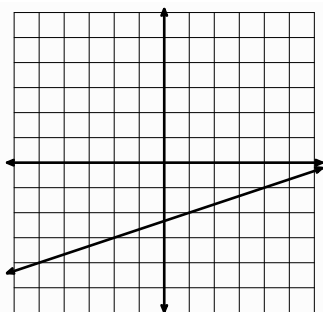
Modeling Data | 8.5

Go

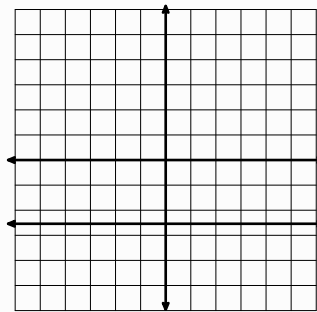
Topic: Visually comparing slopes of lines

Follow the prompt to sketch the graph of a line on the same grid with the given characteristics.

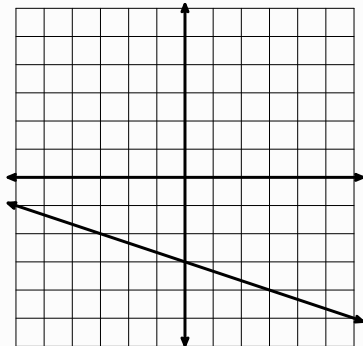
8. A larger slope



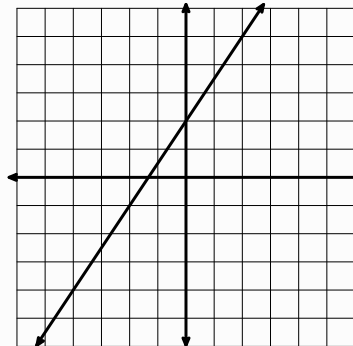
9. A smaller slope



10. A larger y-intercept and a smaller slope



11. Slope is the negative reciprocal



Need Help? Check out these related videos:

<http://www.khanacademy.org/math/algebra/linear-equations-and-inequalitie/v/fitting-a-line-to-data>

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8.6 Making More \$

A Solidify Understanding Task

Each year the U.S. Census Bureau provides income statistics for the United States. In the years from 1990 to 2005, they provided the data in the tables below. (All dollar amounts have been adjusted for the rate of inflation so that they are comparable from year-to-year.)

Year	Median Income for All Men
2005	41196
2004	41464
2003	40987
2002	40595
2001	41280
2000	41996
1999	42580
1998	42240
1997	40406
1996	38894
1995	38607
1994	38215
1993	37712
1992	37528
1991	38145

Year	Median Income for All Women
2005	23970
2004	23989
2003	24065
2002	23710
2001	23564
2000	23551
1999	22977
1998	22403
1997	21759
1996	20957
1995	20253
1994	19158
1993	18751
1992	18725
1991	18649

1. Create a scatter plot of the data for men. What is your estimate of the correlation coefficient for these data?
What is the actual correlation coefficient?
What does it tell you about the relationship between income and years for men?
2. On a separate graph, create a scatter plot of the data for women. What is your estimate of the correlation coefficient for these data?
What is the actual correlation coefficient?
What does it tell you about the relationship between income and years for women?

How does that compare to the data for men?



3. Estimate and draw a line of best fit for each set of data.
 - a. Describe how you estimated the line for men. If you chose to run the line directly through any particular points, describe why you selected them.
 - b. Describe how you estimated the line for women. If you chose to run the line directly through any particular points, describe why you selected them.
4. Write the equation for each of the two lines in slope intercept form.
 - a. Equation for men:

 - b. Equation for women:
5. Use technology to calculate a linear regression for each set of data. Add the regression lines to your scatter plots.
 - a. Linear regression equation for men:

 - b. Linear regression equation for women:
6. Compare your estimated line of best fit to the regression line for men. What does the slope mean in each case? (Include units in your answer.)

7. Compare your estimated line of best fit to the regression line for women. What does the y-intercept mean in each case? (Include units in your answer.)

8. Compare the regression lines for men and women. What do the lines tell us about the income of men vs women in the years from 1991-2005?

9. What do you estimate will be the median income for men and women in 2015?



10. The Census Bureau provided the following statistics for the years from 2006-2011.

Year	Median Income for All Men
2011	37653
2010	38014
2009	38588
2008	39134
2007	41033
2006	41103

Year	Median Income for All Women
2011	23395
2010	23657
2009	24284
2008	23967
2007	25005
2006	24429

With the addition of these data, what would you now estimate the median income of men in 2015 to be? Why?

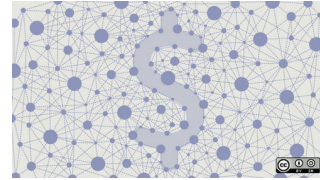
11. How appropriate is a linear model for men's and women's income from 1991-2011? Justify your answer.



Name:

Modeling Data | 8.6

Ready, Set, Go!

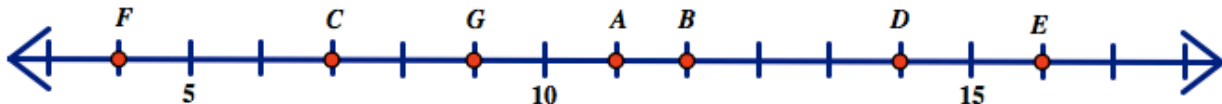


Ready

Topic: Finding distance and averages.

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Use the number line below to answer the questions.



- How far away is each of the points on the number line from *point A*?
(You need to list each point and its distance from *point A*.)
- What is the total of all the distances from *point A* that you found in exercise number one?
- What is the average distance that any of the given *points B through G* are from *point A*?
- Which point on the number line is located the average distance away from *point A*?
- Label another location on the number line that is the average distance away from *point A*.
(Call it *point X*)
- How far away is each of the points on the number line from *point D*?
(You need to list each point and its distance from *point D*.)
- What is the total of all the distances from *point D* that you found in exercise number six?
- What is the average distance that any of the six other points are from *point D*?
- Is there a point on the number line located the average distance away from *point D*?
- Label another location on the number line that is the average distance away from *point D*.
(Call it *point Y*)

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Name:

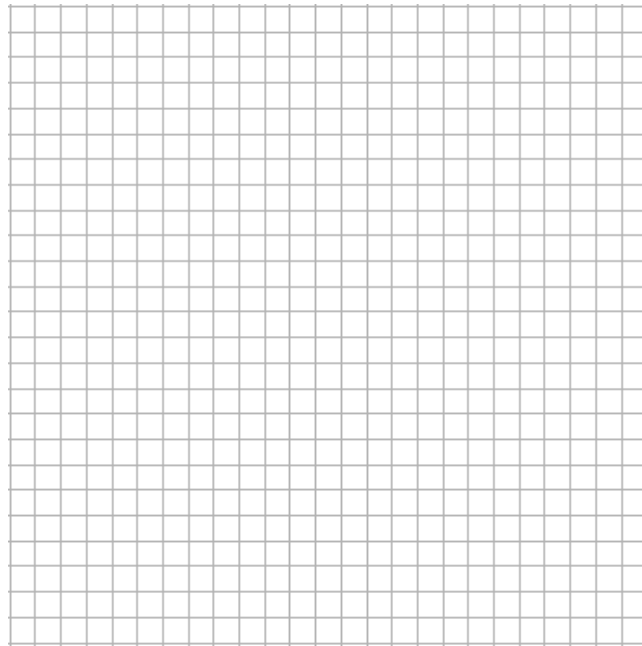
Modeling Data | 8.6

Set

Topic: Scatter Plots and line of best fit or trend lines.

11. Create a scatter plot for the data in the table.

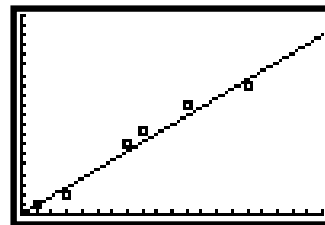
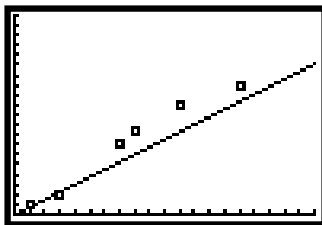
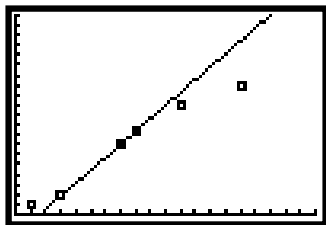
English Score	History Score
60	65
53	59
44	57
61	61
70	67



12. Do the English and History scores have a positive or negative correlation?

13. Do English and History scores have a strong or weak correlation?

14. Which of the graphs below shows the best model for the data and will create the best predictions?
Circle your choice and say why it is the best model for the data.



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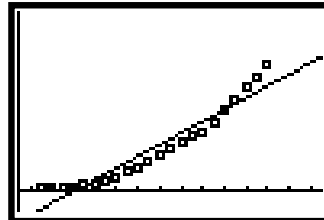
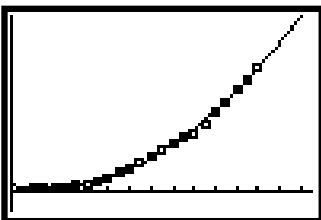
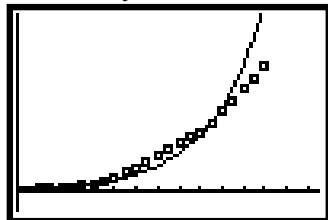
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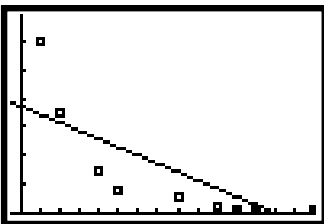
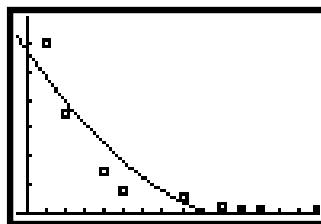
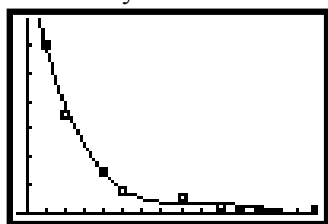
Name:

Modeling Data | 8.6

15. Which of the graphs below shows the best model for the data and will create the best predictions?
Circle your choice and say why it is the best model for the data.



16. Which of the graphs below shows the best model for the data and will create the best predictions?
Circle your choice and say why it is the best model for the data.

**Go**

Topic: Creating explicit functions for arithmetic and geometric sequences.

In each problem below an input connected output are given along with either the common difference or the common ratio. Use this information to create an explicit function for the sequence.

17. $f(2) = 7$, common difference = 3

18. $g(1) = 8$, common ratio = 2

19. $h(6) = 3$, common ratio = -3

20. $r(5) = -3$, common difference = 7

21. $g(7) = 1$, common difference = -9

22. $g(1) = 5$, common ratio = $\frac{1}{2}$

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8.7 Getting Schooled

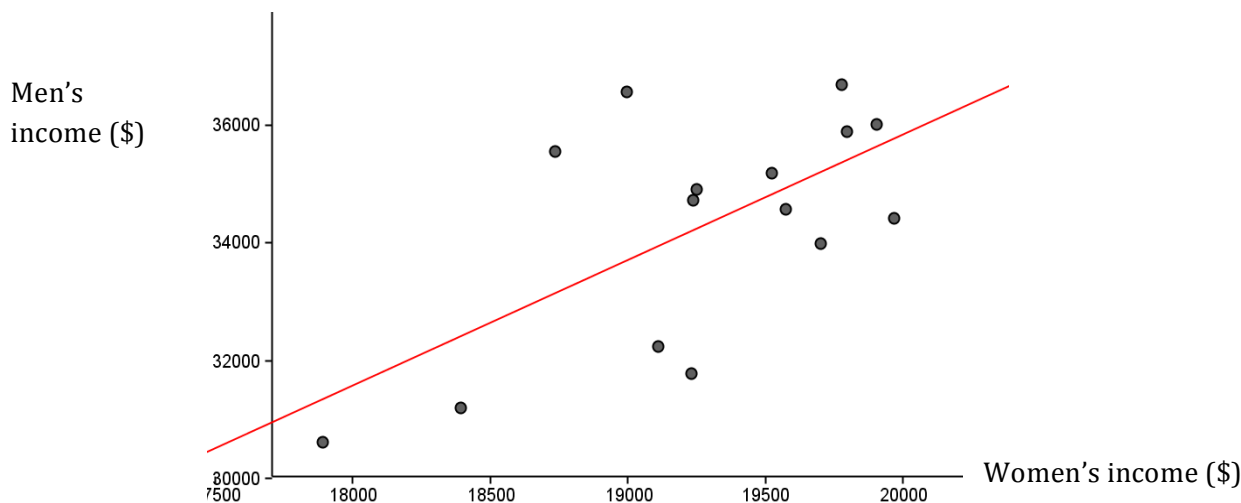
A Solidify Understanding Task



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In *Getting More \$*, Leo and Araceli noticed a difference in men's and women's salaries. Araceli thought that it was unfair that women were paid less than men. Leo thought that there must be some good reason for the discrepancy, so they decided to dig deeper into the Census Bureau's income data to see if they could understand more about these differences.

First, they decided to compare the income of men and women that graduated from high school (or equivalent), but did not pursue further schooling. They created the scatter plot below, with the x value of a point representing the average woman's salary for some year and the y value representing the average man's salary for the same year. For instance, the year 2011 is represented on the graph by the point (17887, 30616). You can find this point on the graph in the bottom left corner.



1. Based upon the graph, estimate the correlation coefficient.
2. Estimate the average income for men in this time period. Describe how you used the graph to find it.
3. What is the average income for women in this time period? Describe how you used the graph to find it.

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4. Leo and Araceli calculated the linear regression for these data to be $y = 2.189x - 6731.8$. What does the slope of this regression line mean about the income of men compared to women? Use precise units and language.

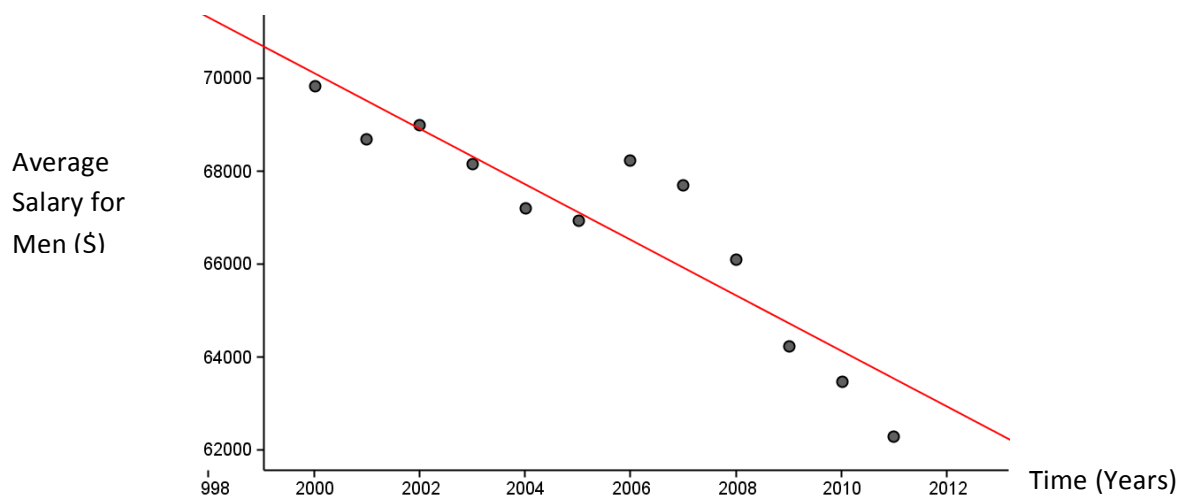
“Hmmm,” said Araceli, “It’s just as I suspected. The whole system is unfair to women.” “No, wait,” said Leo, “Let’s look at incomes for men and women with bachelor’s degrees or more. Maybe it has something to do with levels of education.”

5. Leo and Araceli started with the data for men with bachelor’s degrees or more. They found the correlation coefficient for the average salary vs year from 2000-2011 was $r = -.9145$.

Predict what the graph might look like and draw it here. Be sure to scale and label the axes and put 12 points on your graph.



The actual scatter plot for salaries for men with bachelor's degrees from 2000-2011 is below. How did you do?



- Both Leo and Araceli were surprised at this graph. They calculated the regression line and got $y = -598.25x + 1266626.34$. What does this equation say about the income of men with bachelor's degrees from 2000-2011?
- Leo wondered why the y-intercept in the equation was \$1,266,626.34 and yet the graph seems to cross the y axis around \$72,000. What would you tell Leo to resolve his concern?

Next, they turned their attention to the data for women with bachelor's degrees or more from 2000-2011. Here's the data:

Year	2011	2010	2009	2008	2007	2006	2005	2004	2003	2002	2001	2000
Income for Women (\$)	41338	42409	42746	42620	44161	44007	42690	42539	42954	42871	42992	43293

Analyze these data by creating a scatter plot, interpreting the correlation coefficient and the regression line. Draw the graph and report the results of your analysis below:





Now that you have analyzed the results for women, compare the results for men and women with bachelor's degrees and more over the period from 2000-2011.



Leo believes that the difference in income between men and women may be explained by differences in education, but Araceli believes there must be other factors such as discrimination. Based on the data in this task and *Getting More \$*, make a convincing case to support either Leo or Araceli.

What other data that would be useful in making your case? Explain what you would look for and why.



Name: _____

Modeling Data | 8.7

Ready, Set, Go!

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Ready

Topic: Finding distances and averages.

The graph below has several points and shows the line $y=x$ use this graph to answer each question.

1. The vertical distance between point N and the line $y=x$ is labeled on the graph. Find all of the vertical distances between the points and the line $y = x$.

B:

D:

E:

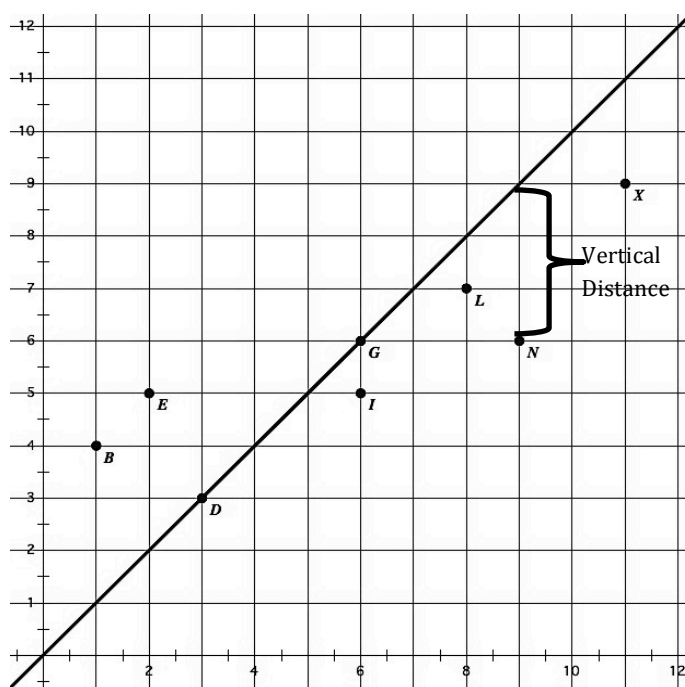
G:

I:

L:

N:

X:



2. What is the *sum of all the distances* that the points are away from the line $y=x$?

3. What is the *average vertical distance* that any of the points are away from the line $y=x$?

4. Is the line on the graph the line of best fit? Explain why or why not. If it is not the best then draw a line that is better fit to the data.

5. Estimate the correlation coefficient for this set of data points.

If you have a way to calculate it exactly then do so. (Using a graphing calculator or data software.)

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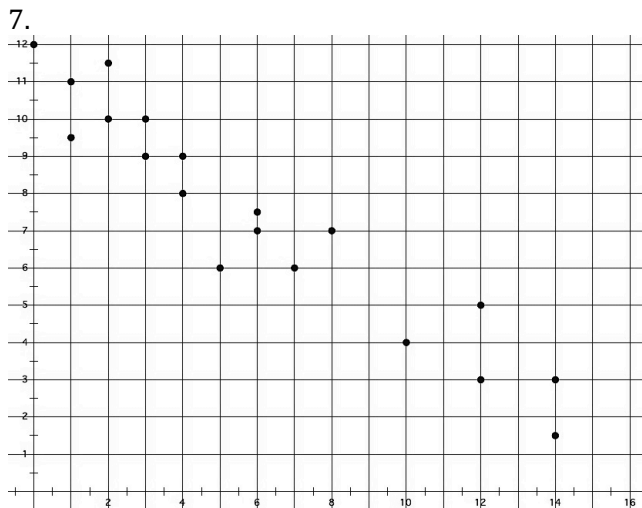
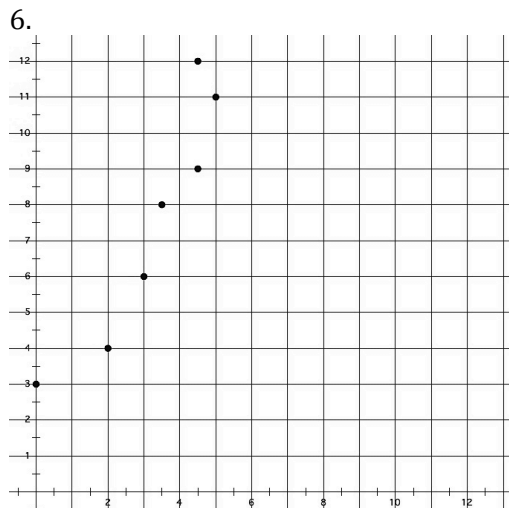
Name: _____

Modeling Data | 8.7

Set

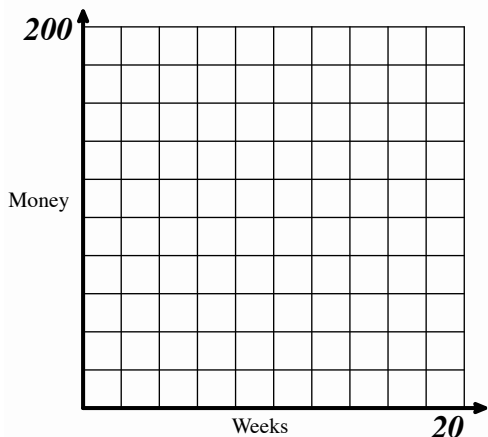
Topic: Creating and analyzing scatter plots.

Determine whether a linear or an exponential model would be best for the given scatter plots. Then sketch a model on the graph that could be used to make predictions.



8a. Use the data to make a scatter plot.

Weeks since school started	Money in savings
1	200
3	175
4	162
7	120
10	87
13	57
20	5



b. Is the correlation of the graph positive or negative? Why?

c. What would you estimate the correlation coefficient to be? Why? (If you have a calculator or software that can calculate it precisely then do so.)

d. Create a regression line and find the regression equation. What is the regression equation?

e. What does the slope of the regression equation mean in terms of the variables?

f. Most school years are 36 weeks. If the rate of spending is kept the same how much more money needs to be saved during the summer in order for there to be money to last all 36 weeks.

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Name:

Modeling Data | 8.7

Go

Topic: Data and statistics, when to use two way tables when to use scatter plots.

9. In what situations does it make the most sense to use a two-way table and look at residual frequencies to make decisions or conclusions?

10. In what situations does it make the most sense to use a scatter plot and a linear or exponential model to analyze and make decisions or draw conclusions?

For each of the representations below label as a *function*, *not a function*. If, *not a function* say why. If it is a function then label as *linear*, *exponential* or *neither*.

11.

x	f(x)
0	5
1	169
2	333
3	497

12.

X	Y
1	15
2	25
3	15
2	30

13.

x	h(x)
2	5
3	10
4	20
5	40

14. $g(x) = 4 - 12x$

15. $s(t) = 3 \cdot 4^{t-1}$

16. The amount of medicine in the blood stream of a cat as time passes. The initial dose of medicine is 80mm and the medicine brakes down at 35% each hour.

17.

Time	0	1	2	3	4
Money in Bank	250	337.50	455.63	615.09	830.38

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8.8 Rockin' the Residuals

A Solidify Understanding Task

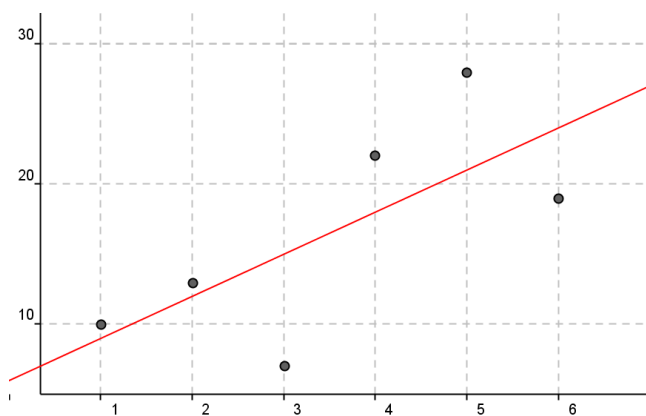
The correlation coefficient is not the only tool that statisticians use to analyze whether or not a line is a good model for the data. They also consider the residuals, which is to look at the difference between the observed value (the data) and the predicted value (the y-value on the regression line). This sounds a little complicated, but it's not really. The residuals are just a way of thinking about how far away the actual data is from the regression line.



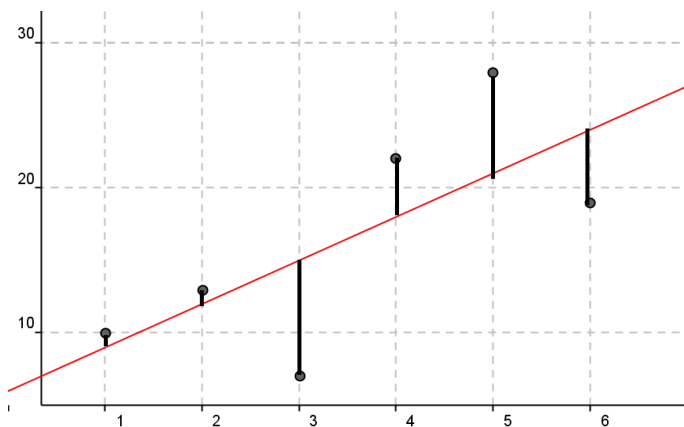
Start with some data:

x	1	2	3	4	5	6
y	10	13	7	22	28	19

Create a scatter plot and graph the regression line. In, this case the line is $y = 3x + 6$.



Draw a line from each data point to the regression line, like the segments drawn from each point below.



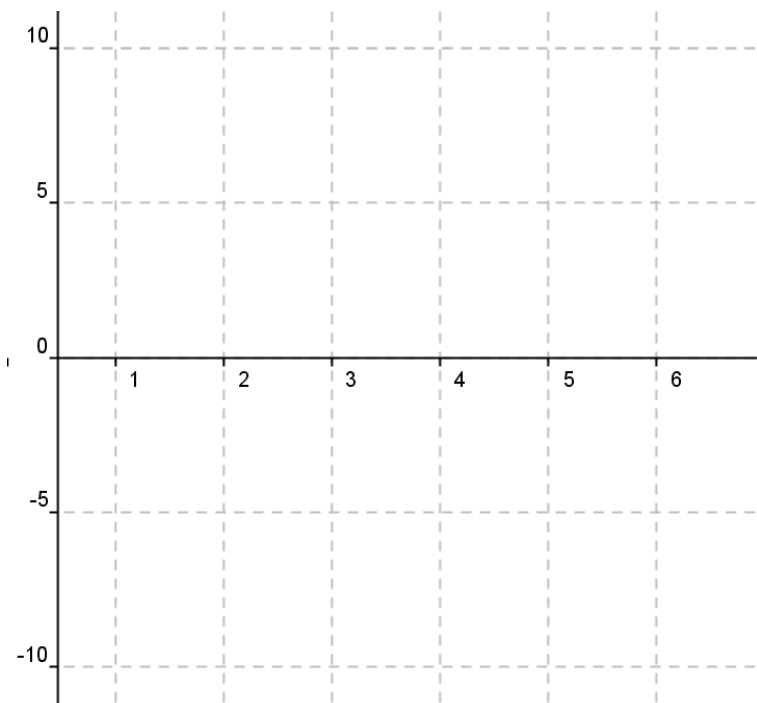
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1. The residuals are the lengths of the segments. How can you calculate the length of each segment to get the residuals?
2. Generally, if the data point is above the regression line the residual is positive, if the data point is below the line, the residual is negative. Knowing this, use your plan from #1 to create a table of residual values using each data point.
3. Statisticians like to look at graphs of the residuals to judge their regression lines. So, you get your chance to do it. Graph the residuals here.



Now, that you have constructed a residual plot, think about what the residuals mean and answer the following questions.

4. If a residual is large and negative, what does it mean?

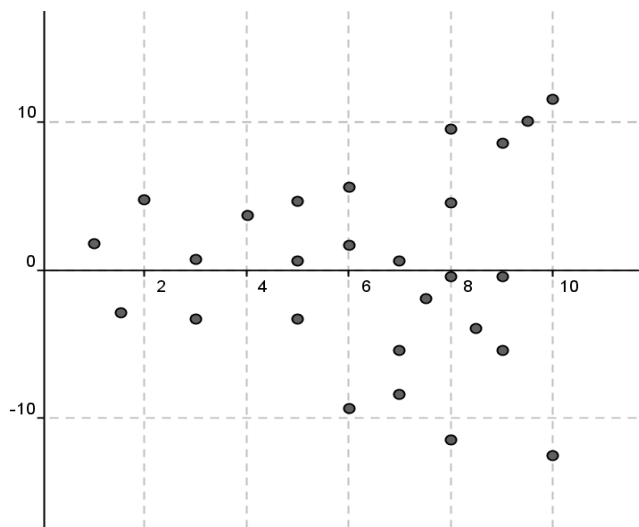
5. What does it mean if a residual is equal to 0?

6. If someone told you that they estimated a line of best fit for a set of data points and all of the residuals were positive, what would you say?

7. If the correlation coefficient for a data set is equal to 1, what will the residual plot look like?

Statisticians use residual plots to see if there are patterns in the data that are not predicted by their model. What patterns can you identify in the following residual plots that might indicate that the regression line is not a good model for the data? Based on the residual plot are there any points that may be considered outliers?

8.



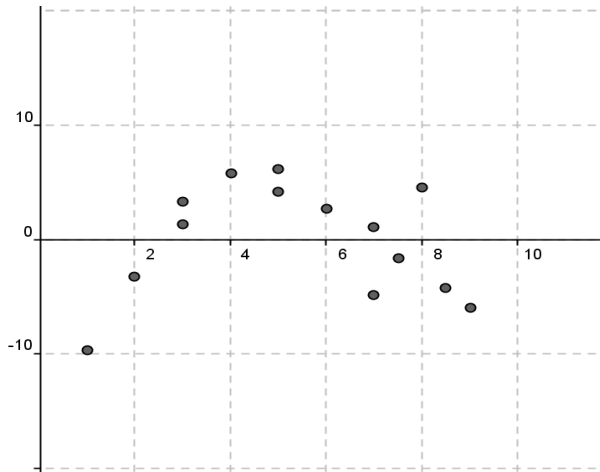
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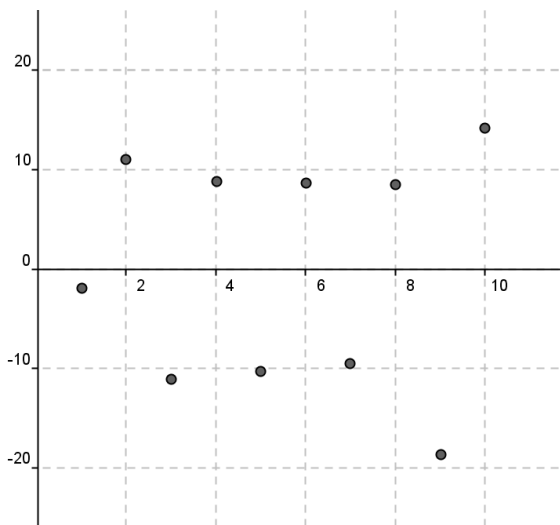
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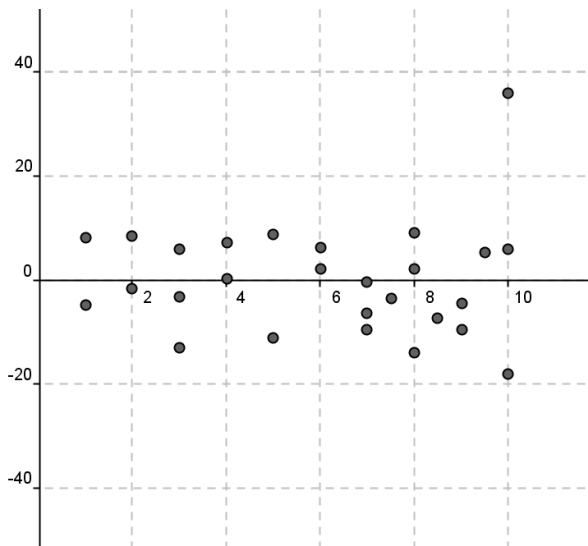
9.



10.



11.



Name: _____

Modeling Data 8.8

Ready, Set, Go!



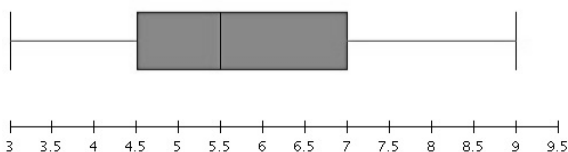
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Ready

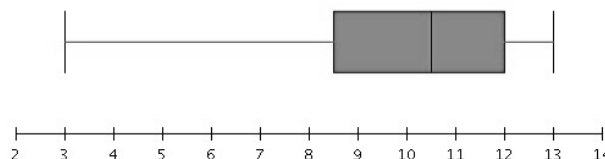
Topic: Describe the spread of the data.

Given the box-and-whisker plots describe the spread of the data set. Provide specifics about the median, range, interquartile range and so forth.

1.

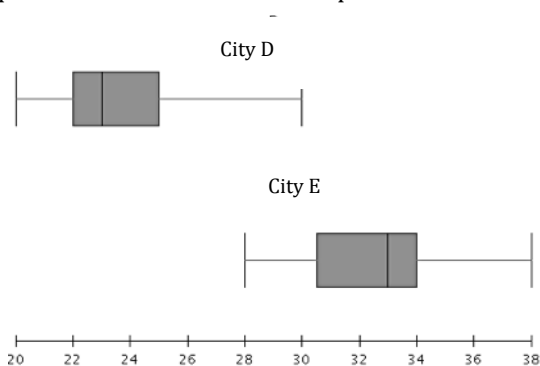


2.



3. If the box-and-whisker plots above represent the results of two different classes on the same assessment, which class did better? Why?

4. The two box-and-whisker plots below show the low temperatures for two cities in the United States.



- Which city would be considered the coldest City D or City E? Why?
- Do these cities ever experience the same temperature? How do you know?
- Is there any way to know the exact temperature for any given day from the box and whisker plots?
- What advantage if any could a scatter plot of temperature data have over a box and whisker plot?



Name: _____

Modeling Data | 8.8

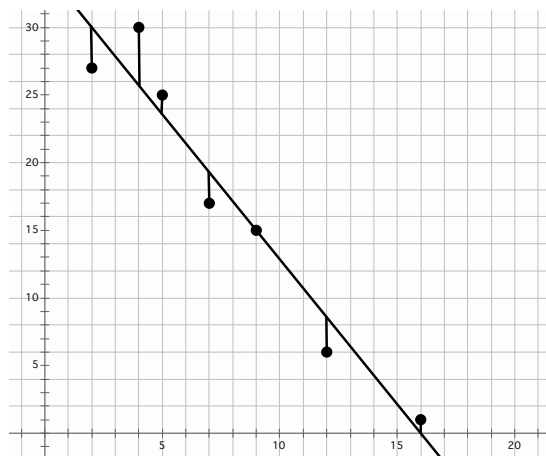
Set

Topic: Residuals, residual plots and correlation coefficients.

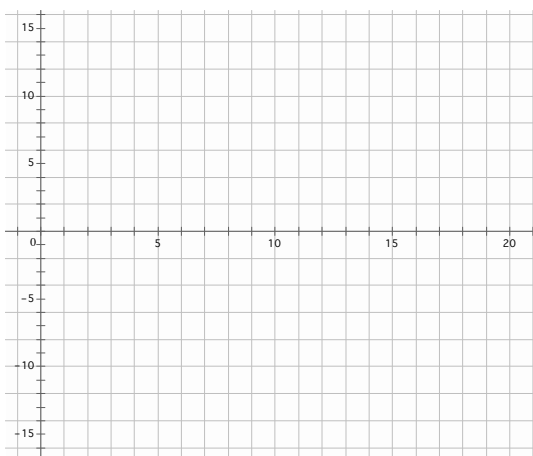
The Data Sheets below are scatter plots that have the regression line and the residuals indicated.

- 5a. Mark on the graph where (\bar{x}, \bar{y}) would be located.
- b. Use this given plot to create a residual plot.
- c. What would you predict the correlation coefficient to be?

Data Sheet 1

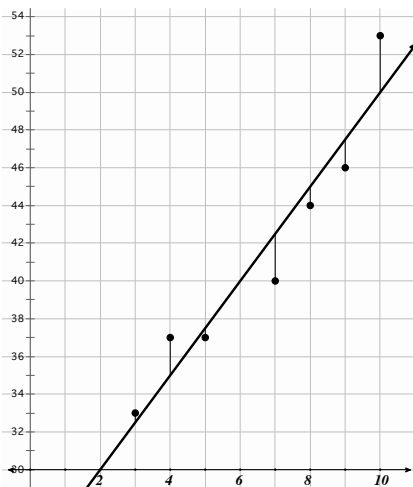


Residual Plot 1

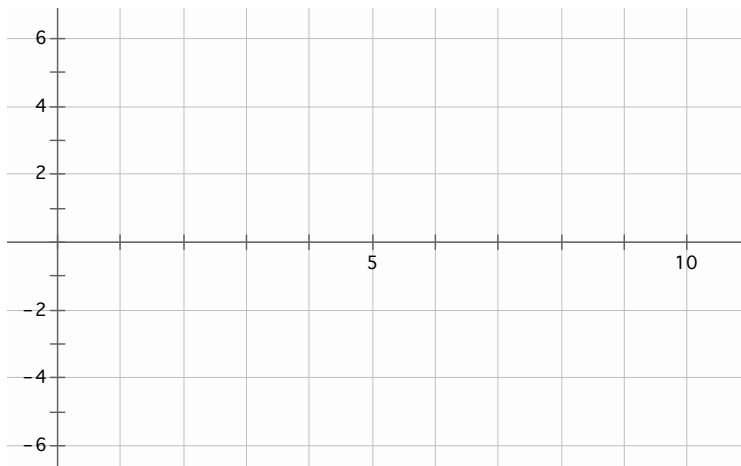


- 6a. Mark on the graph where (\bar{x}, \bar{y}) would be located.
- b. Use this given plot to create a residual plot.
- c. What would you predict the correlation coefficient to be?

Data Sheet 2



Residual Plot 2



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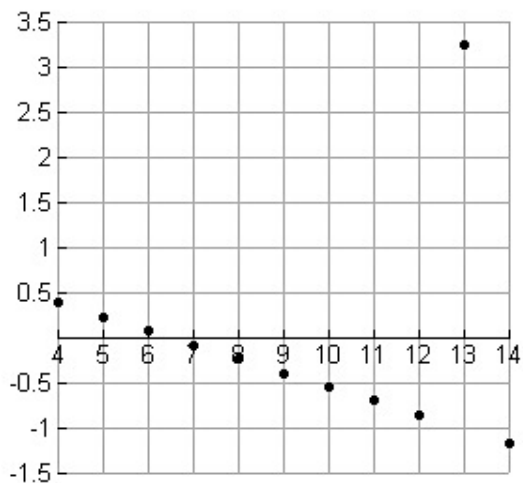


Name:

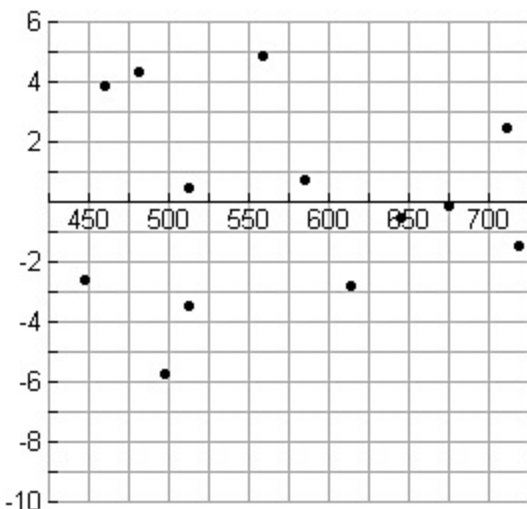
Modeling Data | 8.8

The following graphs are residual plots. Analyze the residual plots to determine how well the prediction line (line of best fit) describes the data.

7. Plot 1

Analysis

8. Plot 2

Analysis

Name:

Modeling Data | 8.8

Go

Topic: Geometric constructions.

9. Construct an isosceles triangle with a compass and straight edge.

10. Construct a square using compass and straight edge..

11. Use a compass and straight edge to construct a hexagon inscribed in a circle.

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